

# **Direct Numerical Simulation of Of Dense Gas-Solid Flows Including Particle Collision**

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**NETL 2011 Workshop On Multiphase Flow Science**

# Outline

- Motivation and Objectives
- Governing Equations
- Results
  - Fluctuation Velocities
  - Particle Concentration
  - Particle Deposition Velocity
- Conclusions

# Objectives

**Provide insight into the following questions:**

- **How the particle and flow turbulence intensities are affected?**
- **How the particle deposition velocity is affected by two-way coupling, particle collisions and four-way coupling?**
- **How the particle-velocity correlations are affected by increase in concentration?**

# Direct Numerical Simulations

## Wall Units

$$u_i^+ = \frac{u_i}{u^*}$$

$$x_i^+ = \frac{u^* x_i}{v}$$

## Navier-Stokes

$$\nabla^+ \cdot \mathbf{u}^+ = 0$$

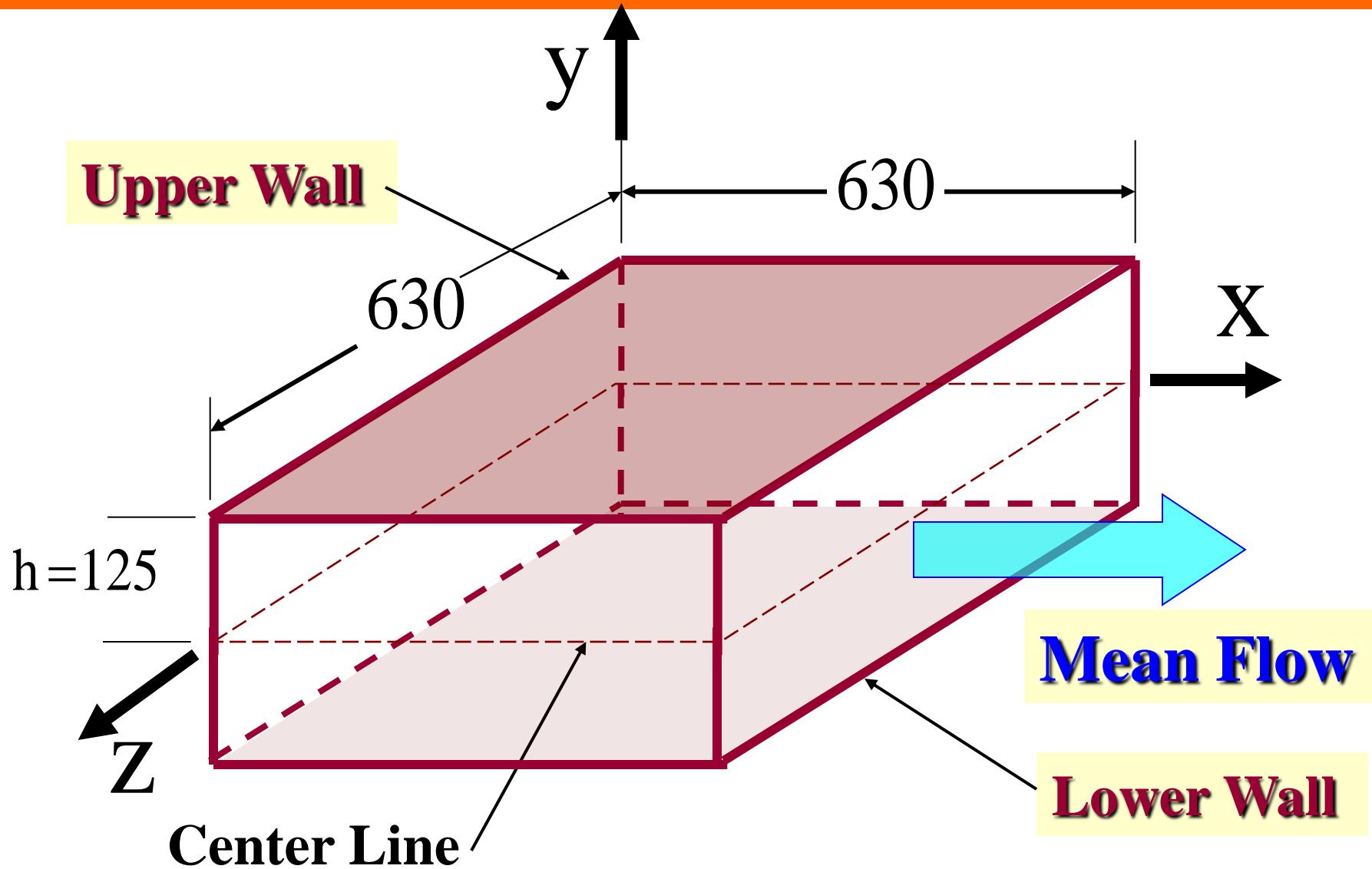
$$\frac{\partial \mathbf{u}^+}{\partial t^+} + \mathbf{u}^+ \cdot \nabla^+ \mathbf{u}^+ = \nabla^{+2} \mathbf{u}^+ - \nabla^+ P^+ + S_u^p$$

# Spectral Method

$$\vec{u}(x, y, z, t) = \sum_{l=-\frac{N_x}{2}}^{\frac{N_x}{2}-1} \sum_{m=-\frac{N_z}{2}}^{\frac{N_z}{2}-1} \sum_{n=0}^{N_y} \tilde{\vec{v}}(l, m, n, t) e^{2\pi i (\frac{lx}{\lambda_x} + \frac{mz}{\lambda_z})} T_n\left(\frac{y}{H}\right)$$

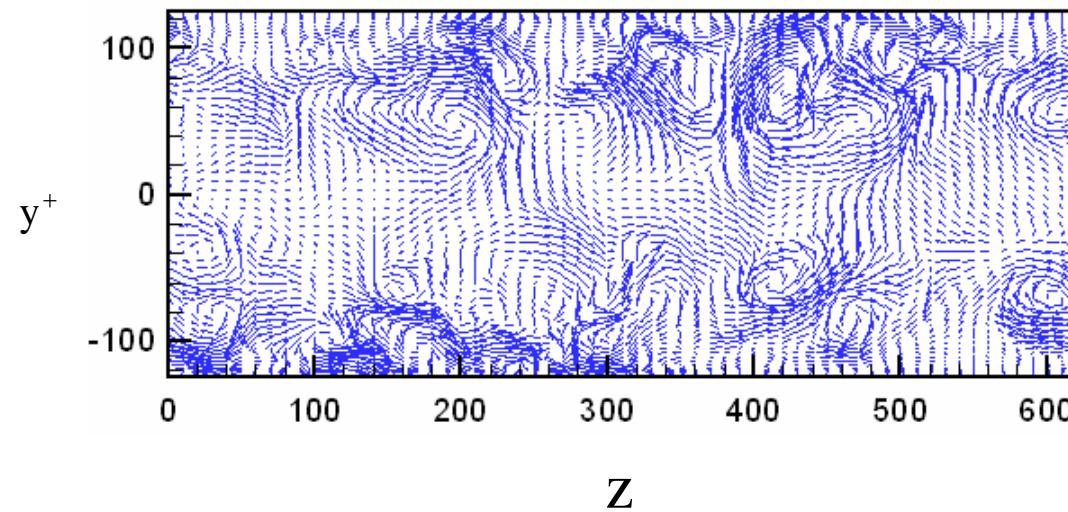
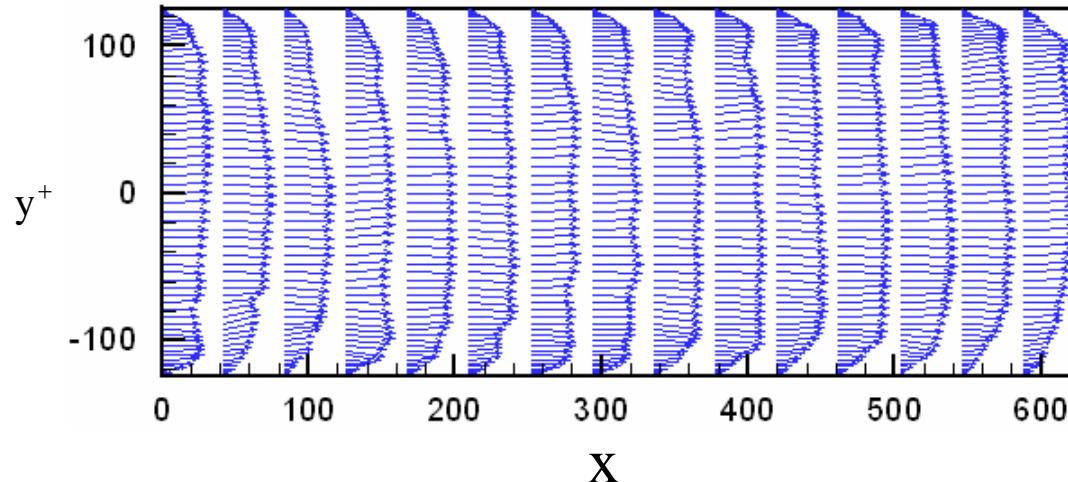
$$T_n\left(\frac{y}{H}\right) = \cos\left(n \cos^{-1}\left(\frac{y}{H}\right)\right)$$

# Flow Between Two Parallel Plates



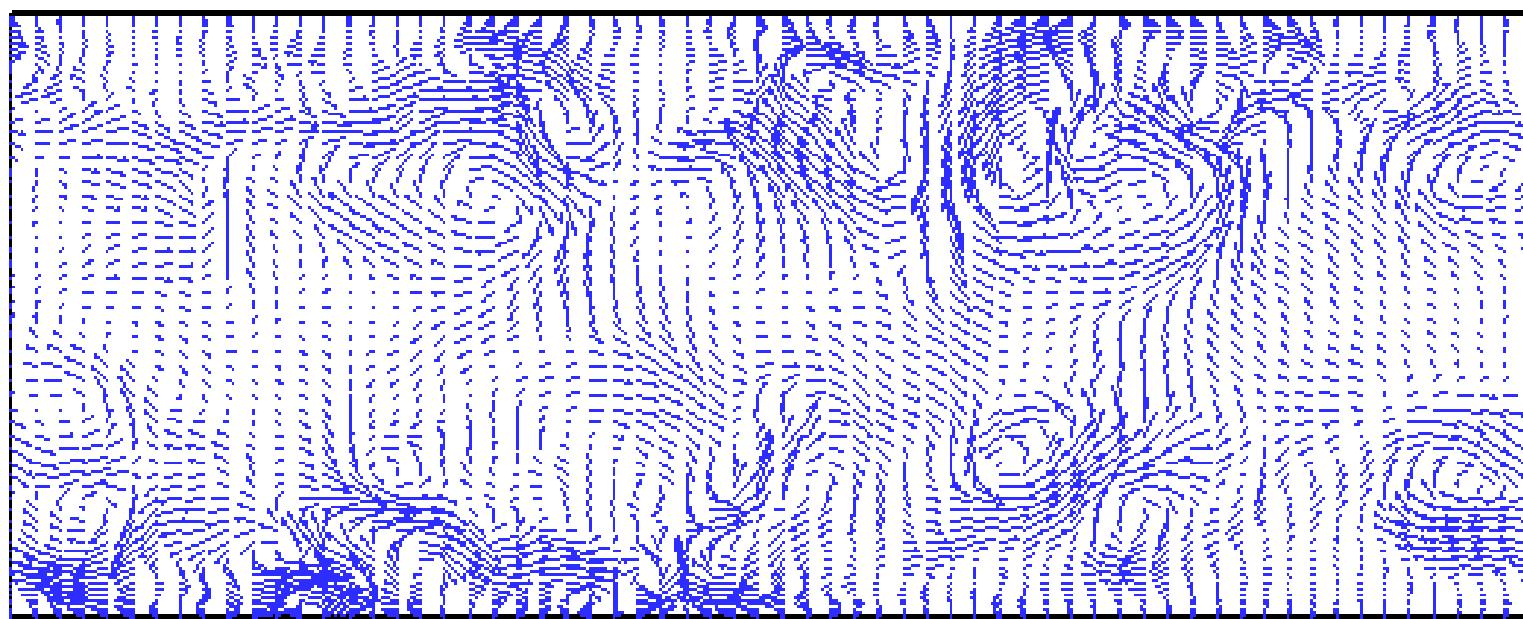
# Instantaneous Velocity Field

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# Flow Field Visualization

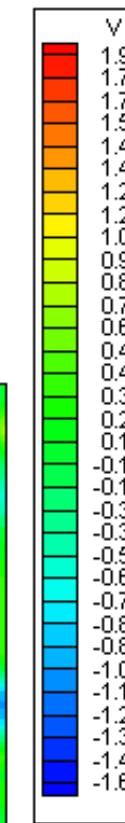
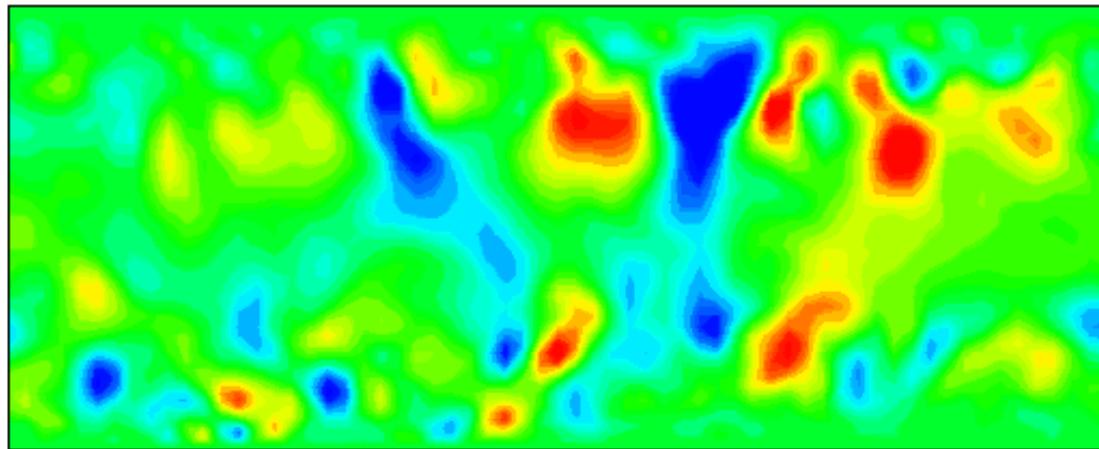
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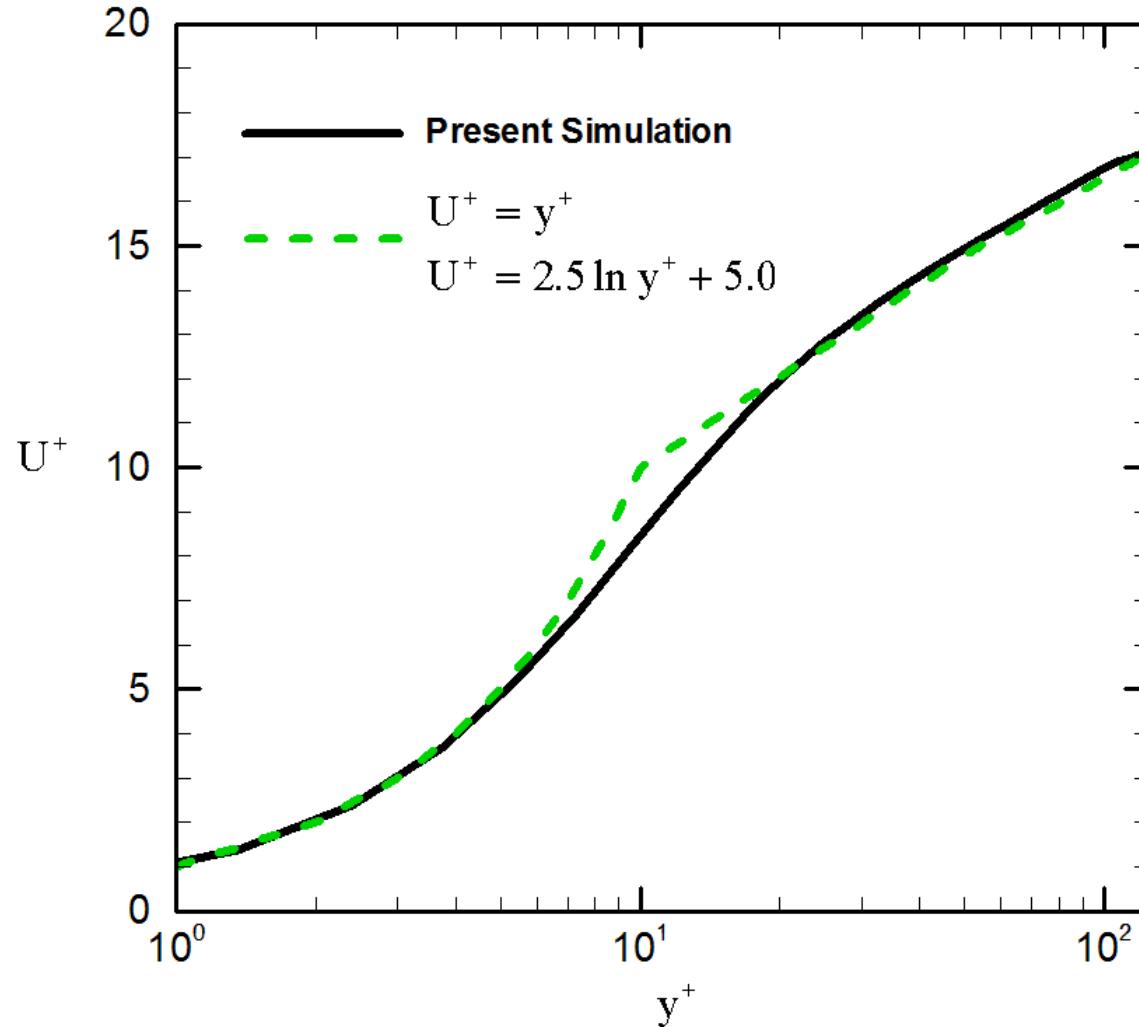
# Contour Plot of v-Velocity

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vertical velocity contour



# Average Streamwise Velocity



# Particle Equations

$$\frac{d\vec{u}^{+p}}{dt^+} = C_D F_d^+ + F_l^+ + \vec{n}^+(t^+) + \vec{g}^+$$

$$\frac{d\vec{x}^+}{dt^+} = \vec{u}^{+p}$$

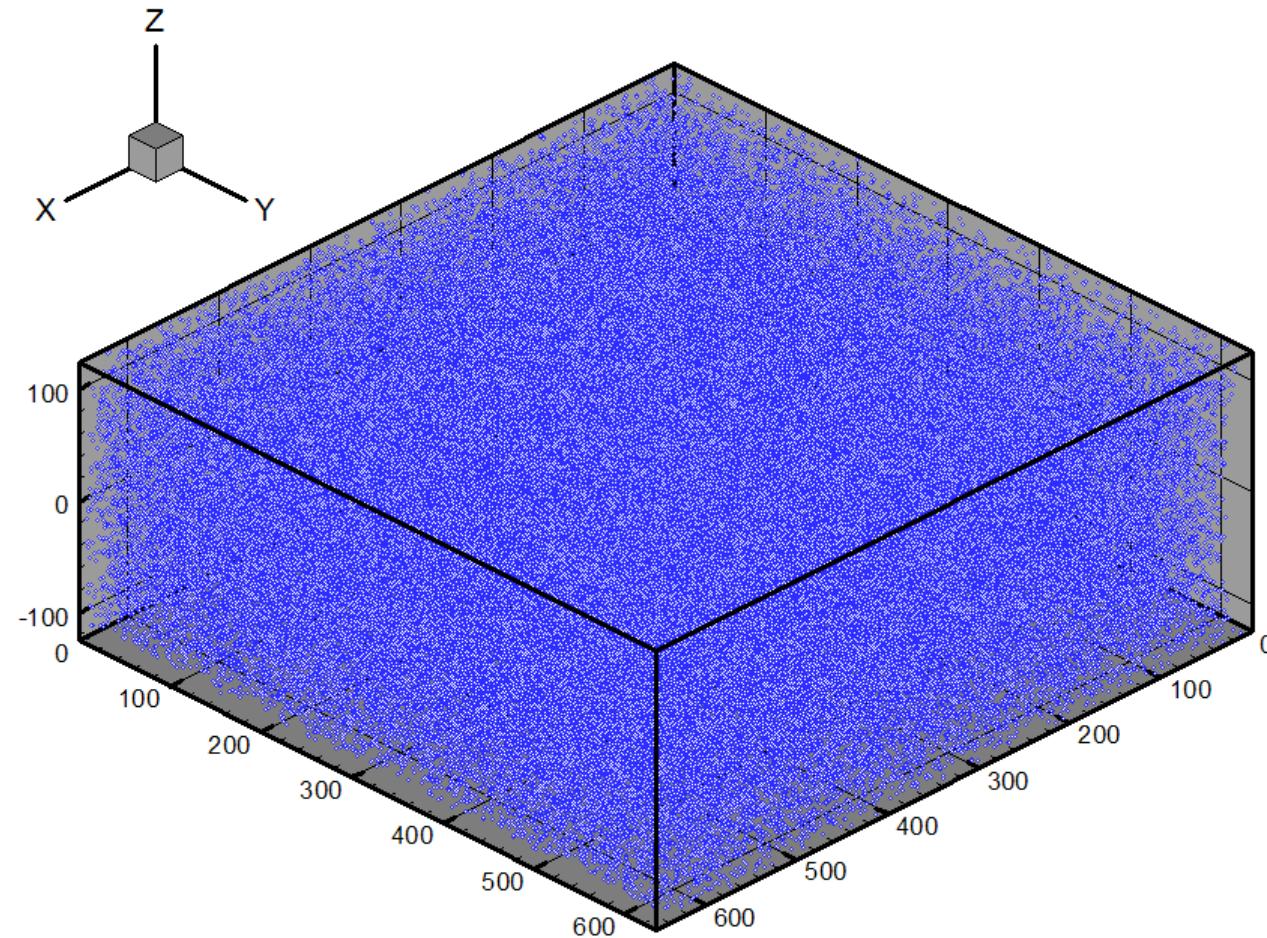
$$C_D = \begin{cases} 1.0 + 0.1875 Re_p & Re_p \leq 0.01 \\ 1.0 + 0.1315 Re_p^{0.82 - 0.0217 \ln(Re_p)} & 0.01 \leq Re_p \leq 20 \end{cases}$$

Wall units

$$\vec{x}^+ = \frac{\vec{x} u^*}{\nu} \quad t^+ = \frac{t u^{*2}}{\nu} \quad \vec{u}^+ = \frac{\vec{u}}{u^*}$$

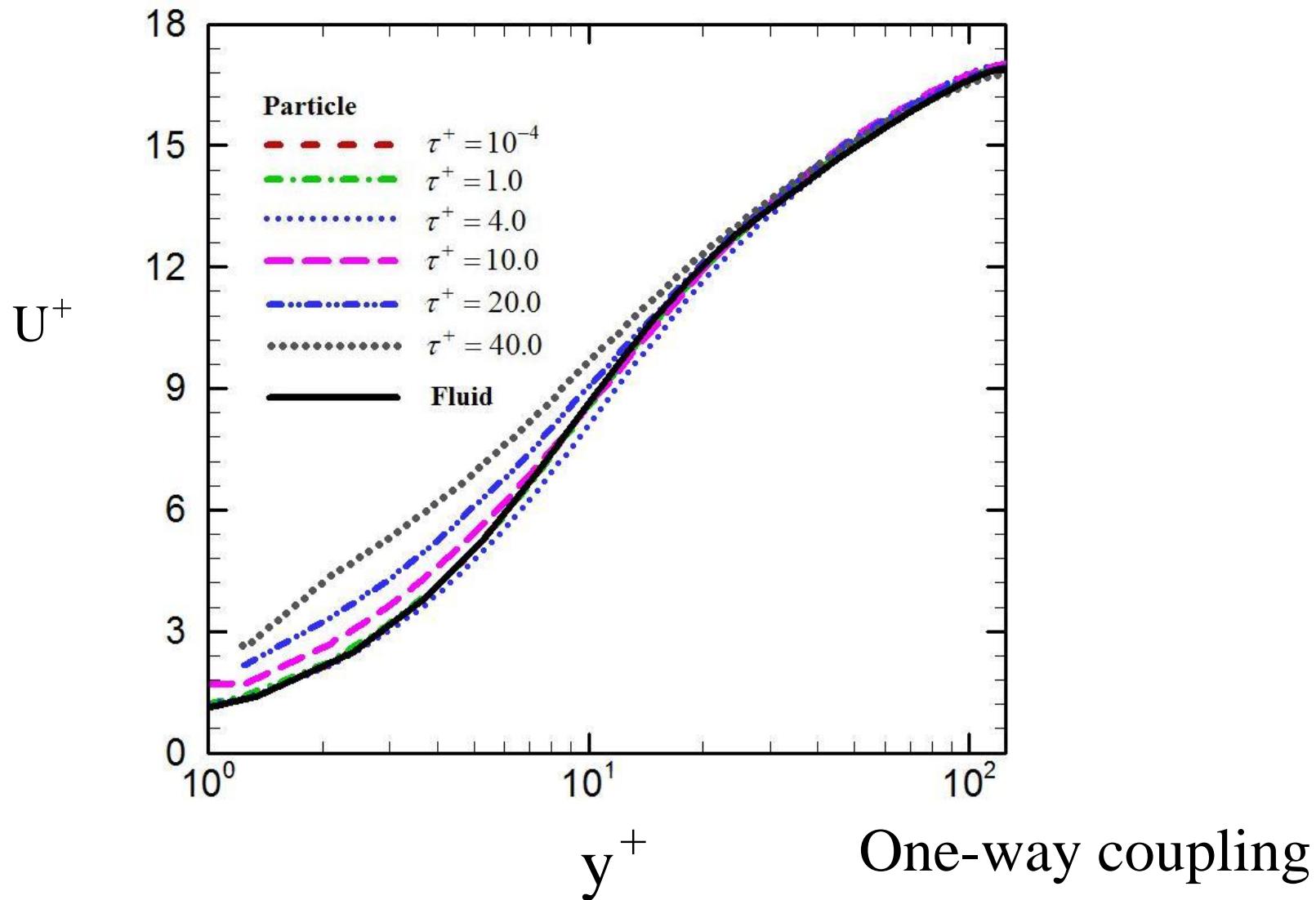
Point Particles approximations, inelastic collisions

# Initial Particle Distribution

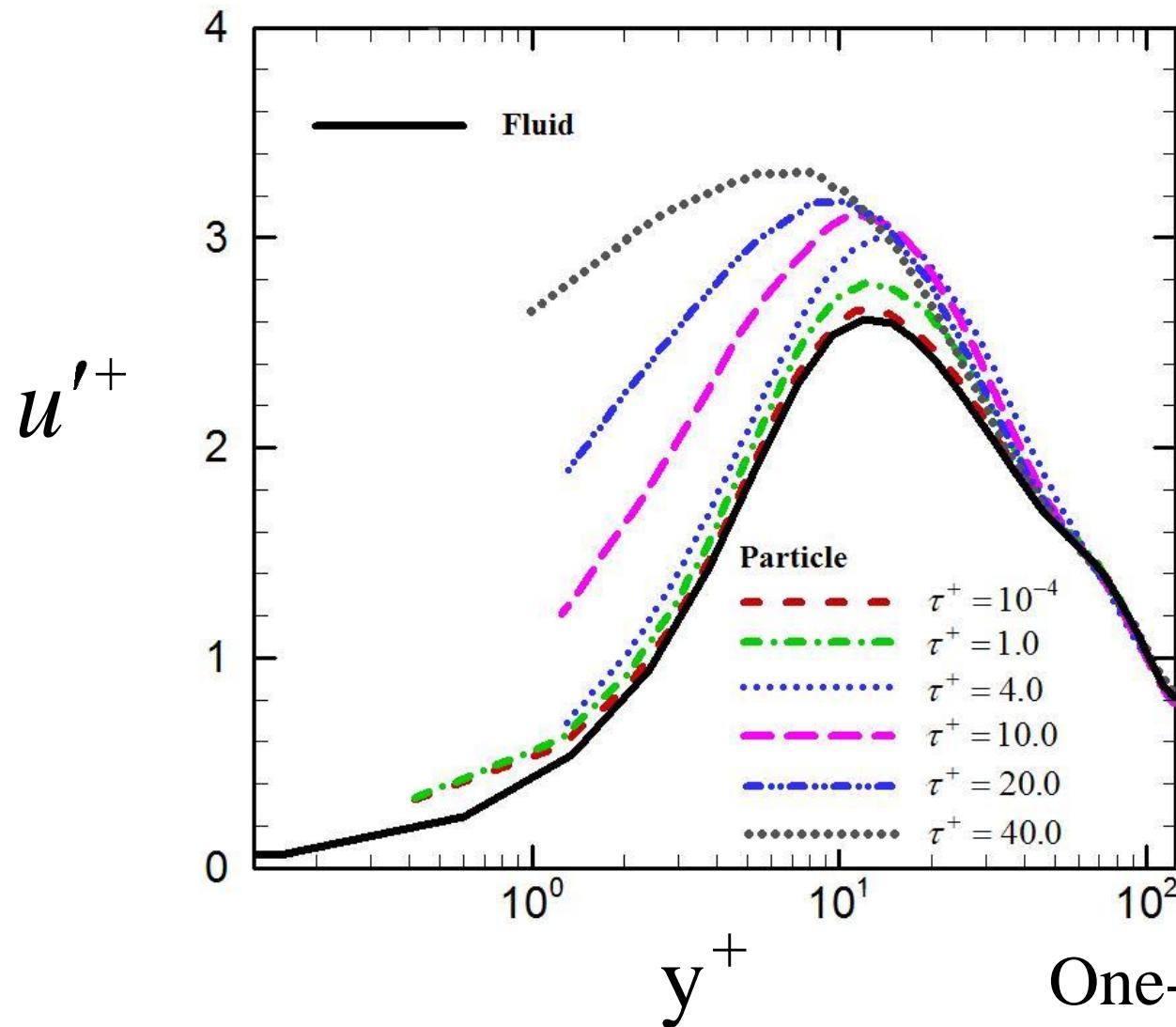


# Particle Streamwise Mean Velocity

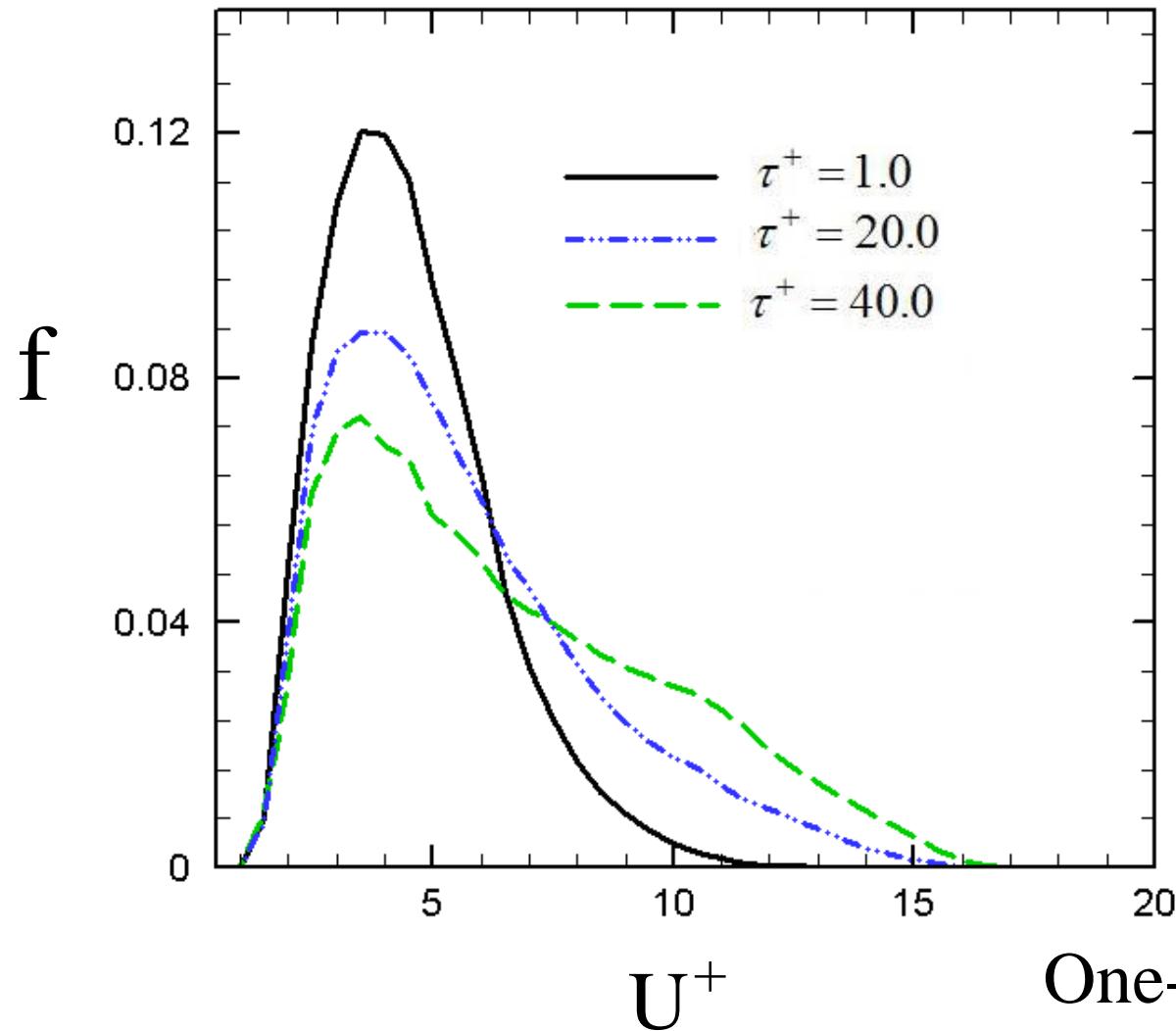
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# Fluid and Particle Streamwise Fluctuating Velocities



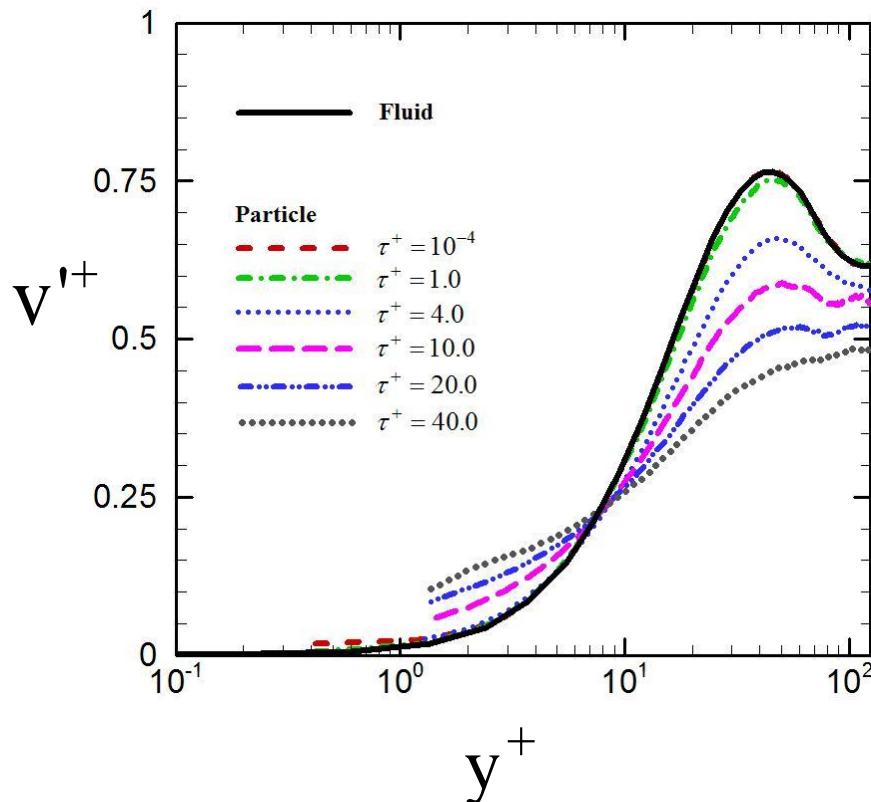
# Velocity Distribution of Particles in $5 < y^+ < 7$



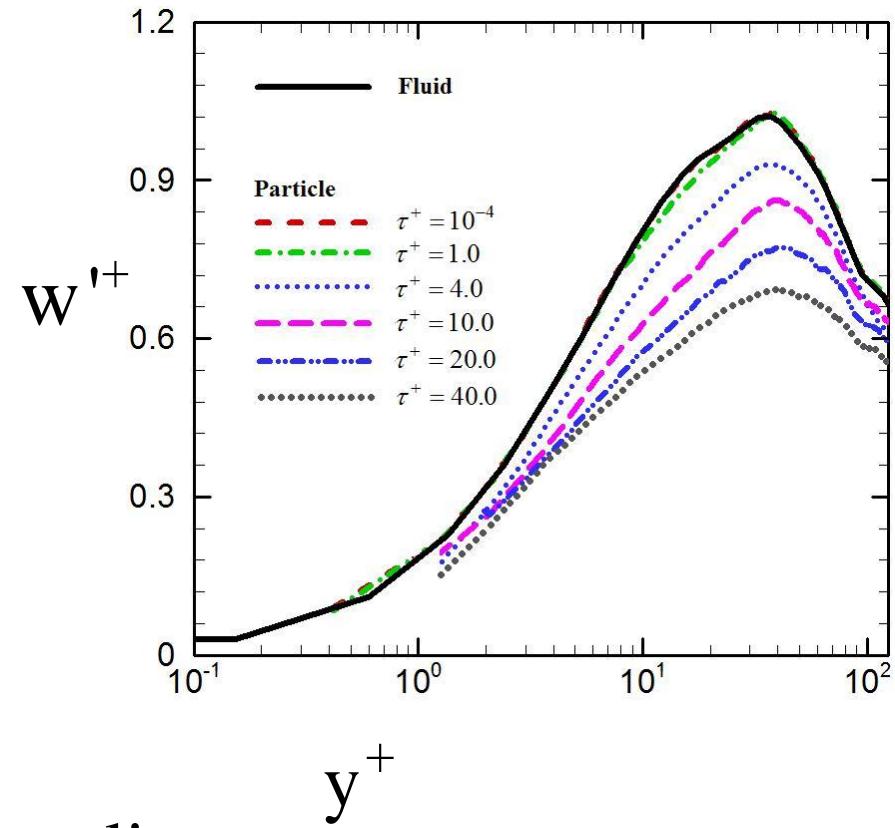
# Fluctuating Velocities

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## Normal fluctuating velocity



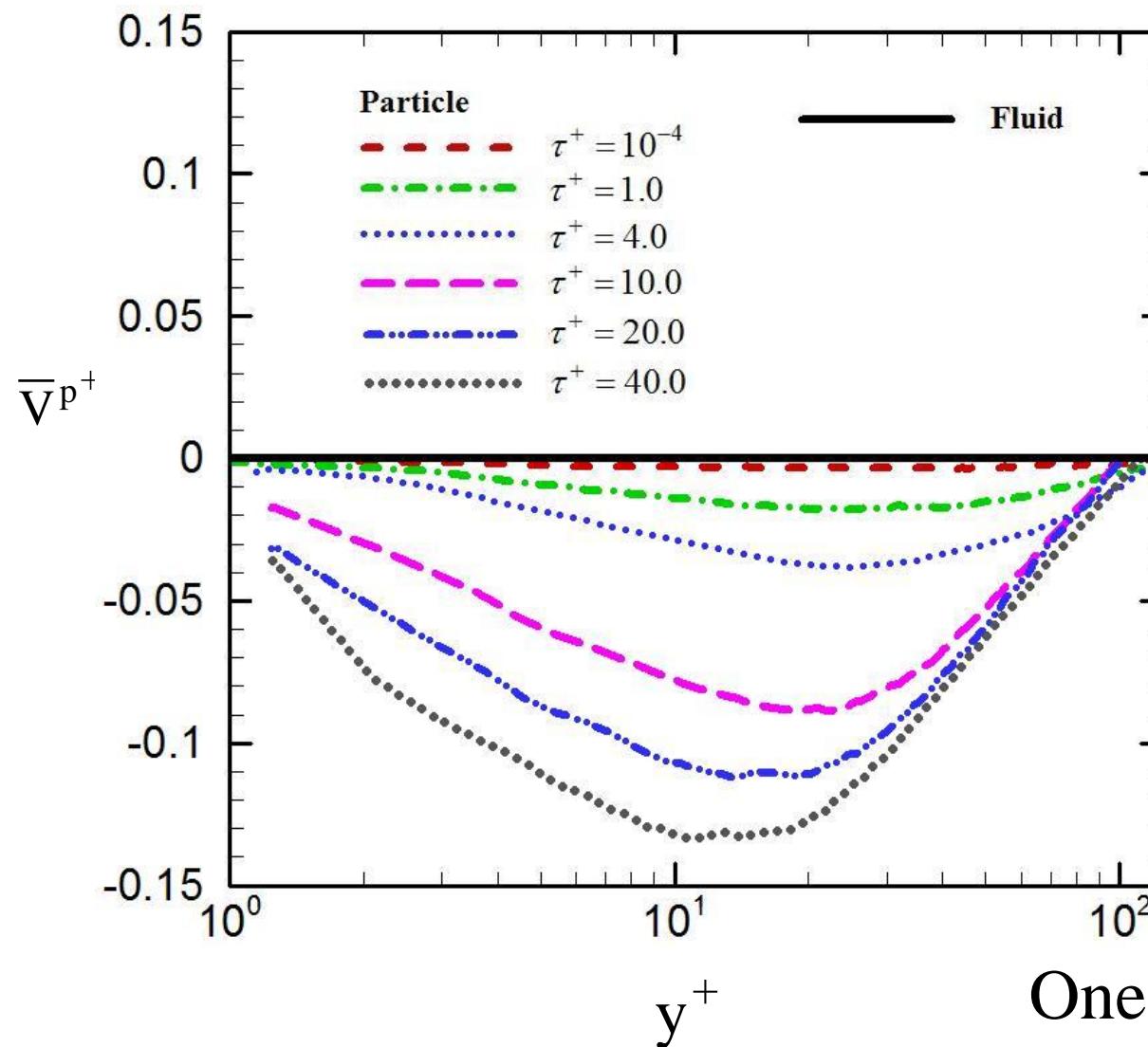
## Spanwise fluctuating velocity



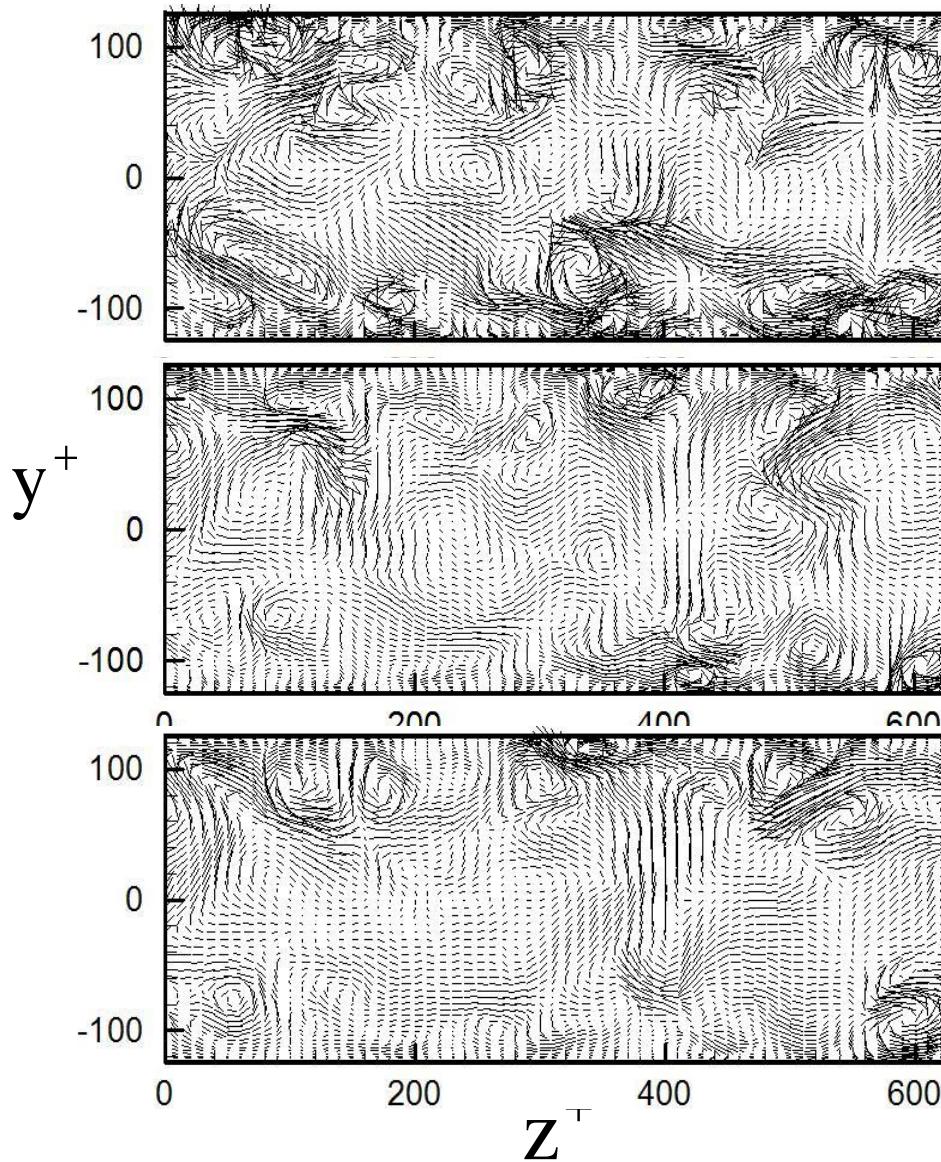
One-way coupling

# Particle Flux Toward Wall (Turbophoresis)

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# Sample Velocity Vector Plots

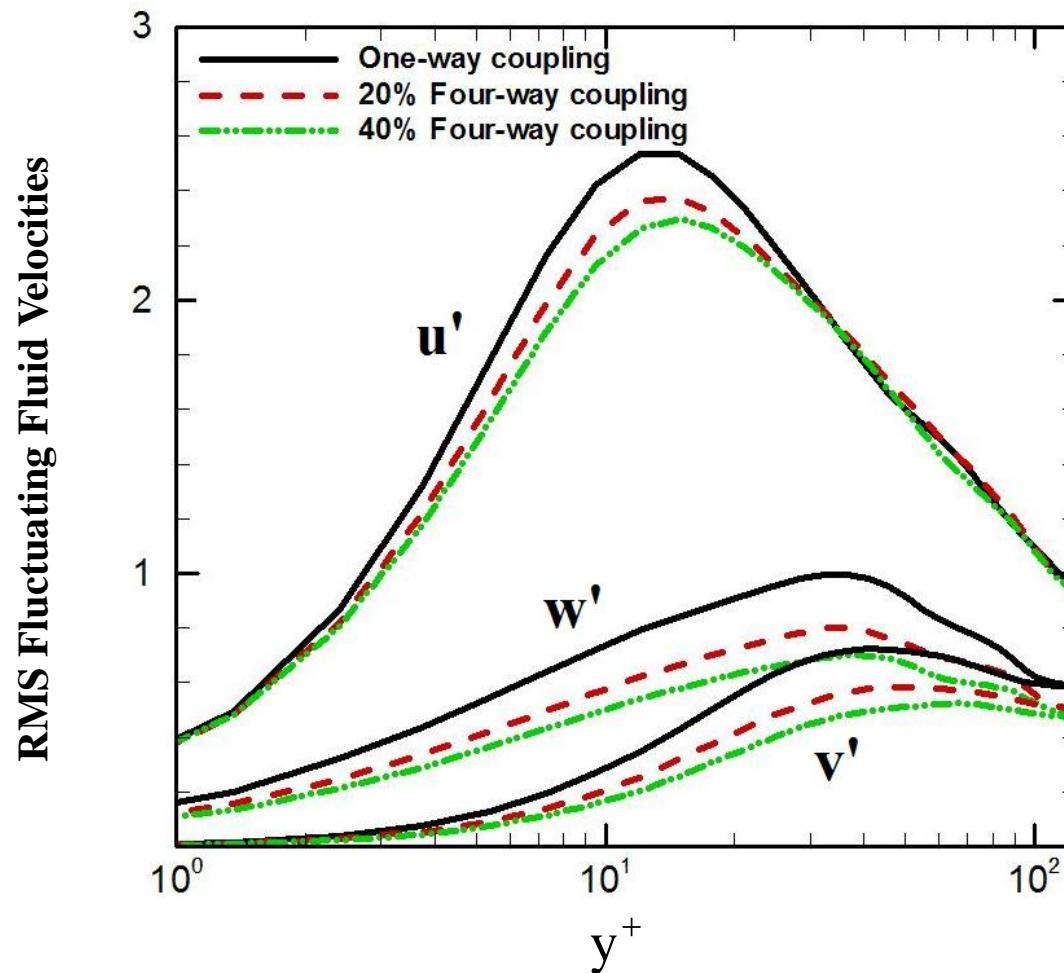


**One-way coupling**

**Four-way coupling,  
M.L.=20%**

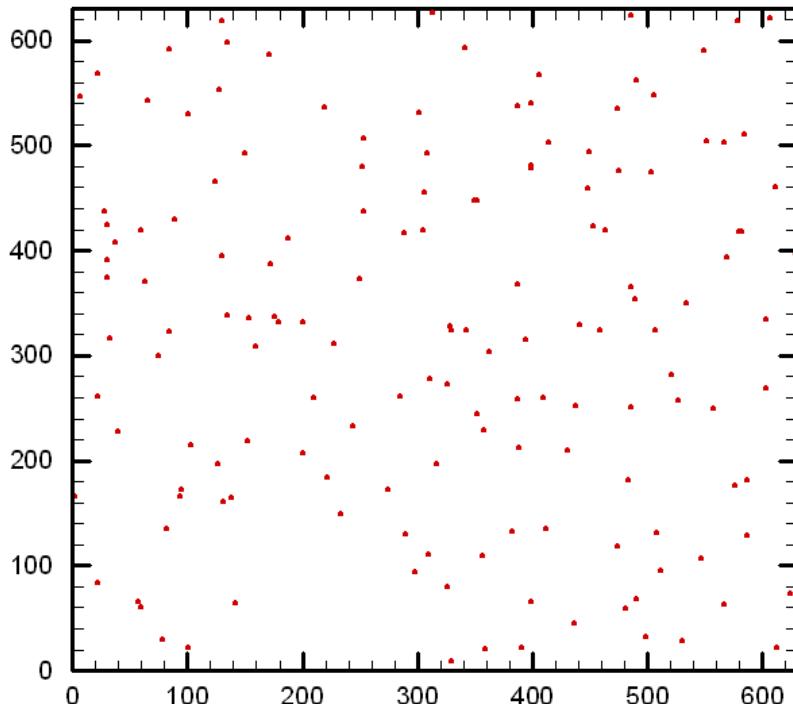
**Four-way coupling,  
M.L.=40%**

# RMS Velocities

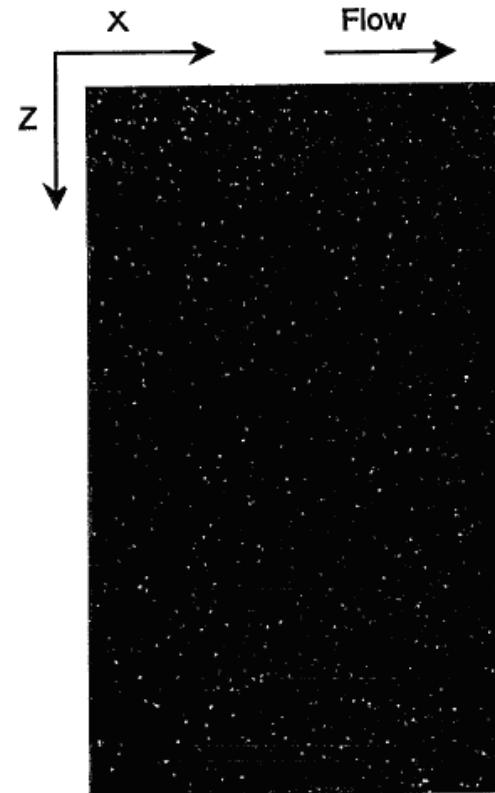


Effects of  $d=30$  micron particles on the flow fluctuating velocities.

# Particle Distribution

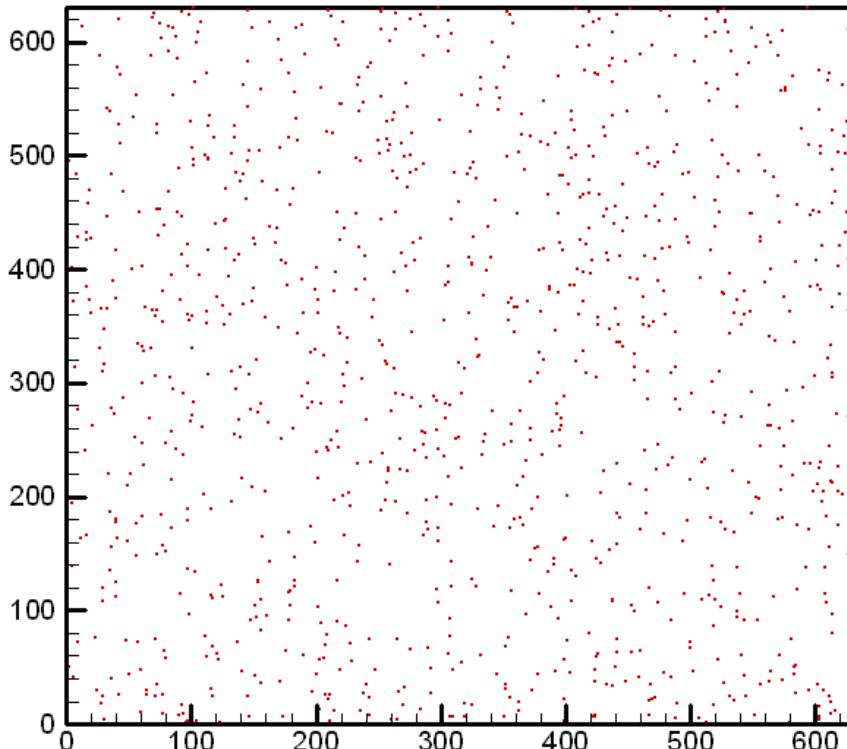


Fessler et al. (1994)

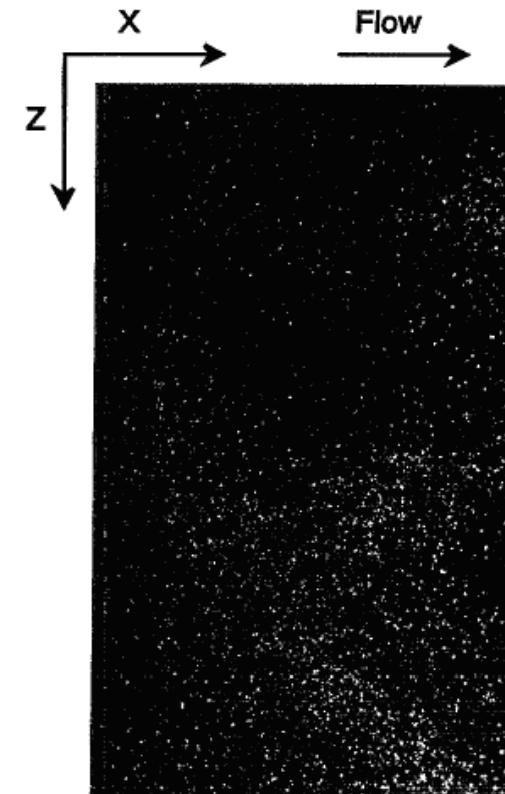


**Distribution of 70 micron copper particles  
(S=7333) at the channel center-plane.**

# Particle Distribution

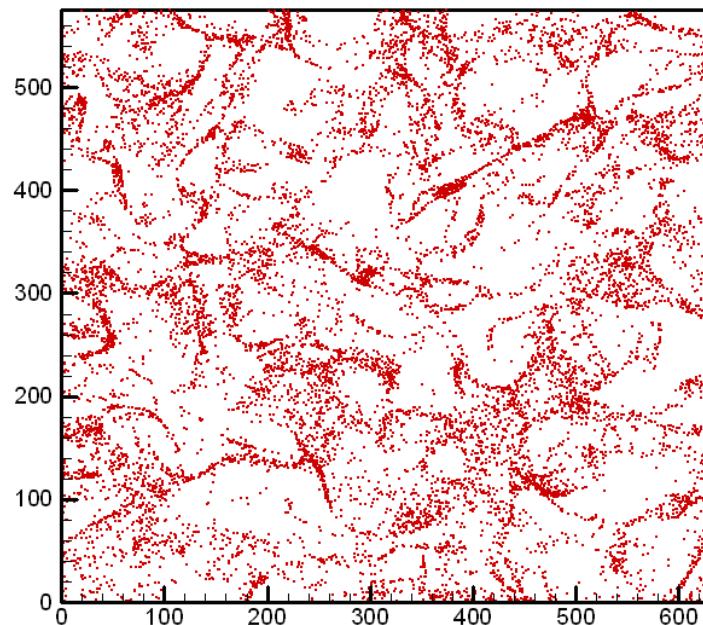


Fessler et al. (1994)

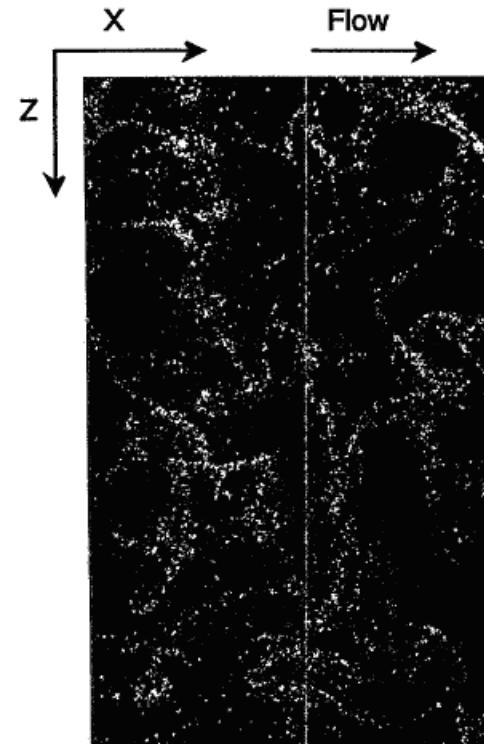


**Distribution of 50 micron glass particles ( $S=2030$ ) at the channel center-plane**

# Particle Distribution



Fessler et al. (1994)



**Distribution of 28 micron Lycopodium particles ( $S=826$ ) at the channel center-plane**

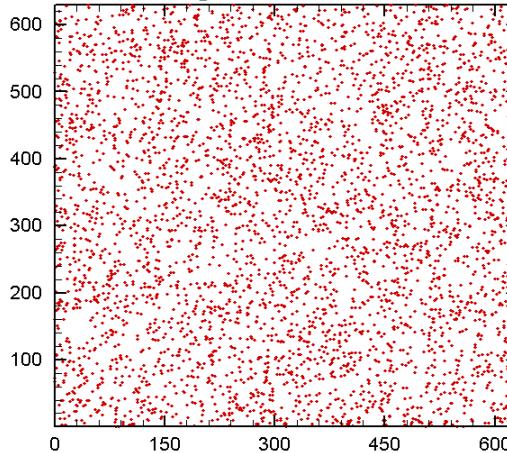
# Particle Distribution

**The lack of preferential concentration for copper and glass particles could be due to**

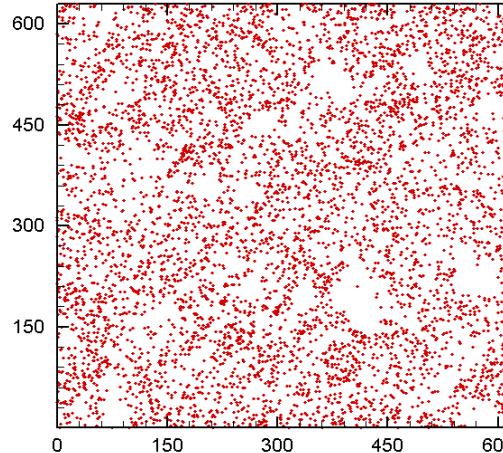
- **Particle High Stokes number**
- **Inter-particle collisions**

# Particle Distribution at the channel center-plane

$$\tau_p^+ = 10^{-4}$$

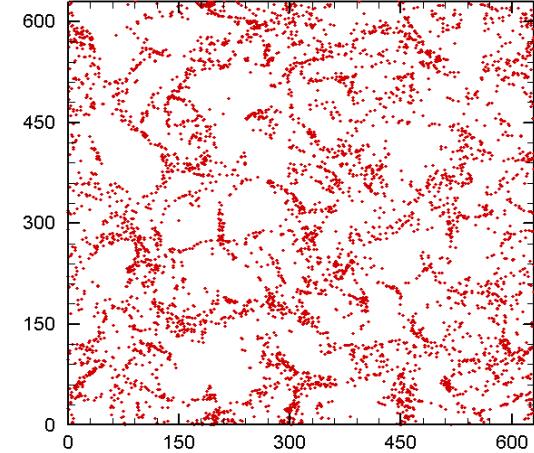


$$\tau_p^+ = 1.0$$

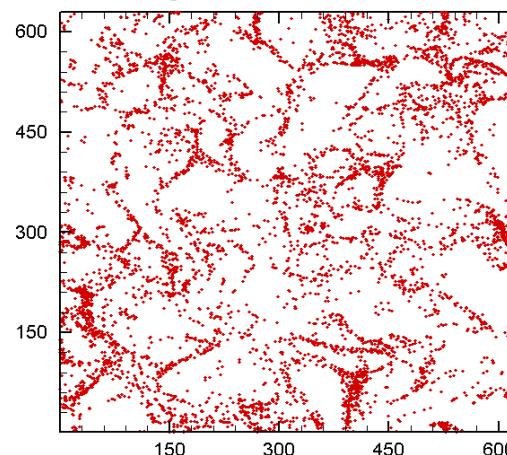


One Way Coupling

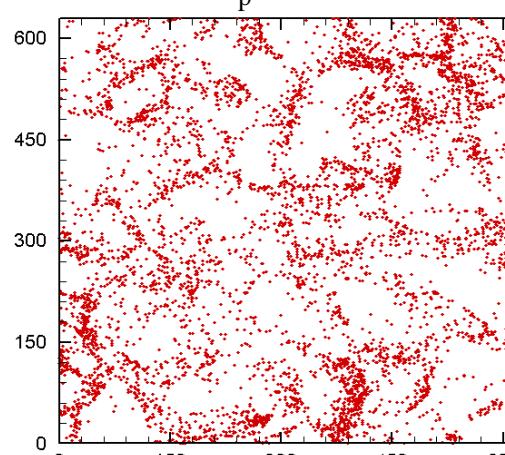
$$\tau_p^+ = 4.4$$



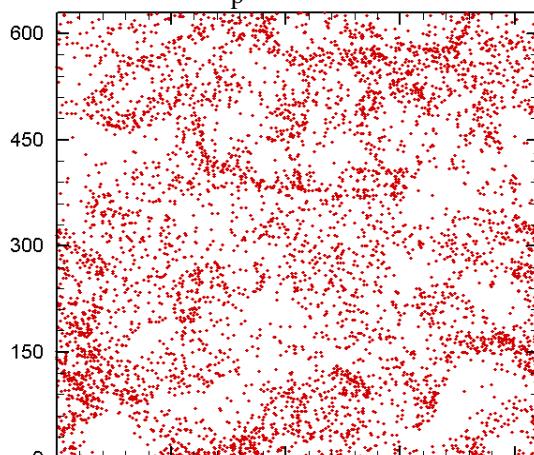
$$\tau_p^+ = 10.0$$



$$\tau_p^+ = 20$$



$$\tau_p^+ = 40.0$$

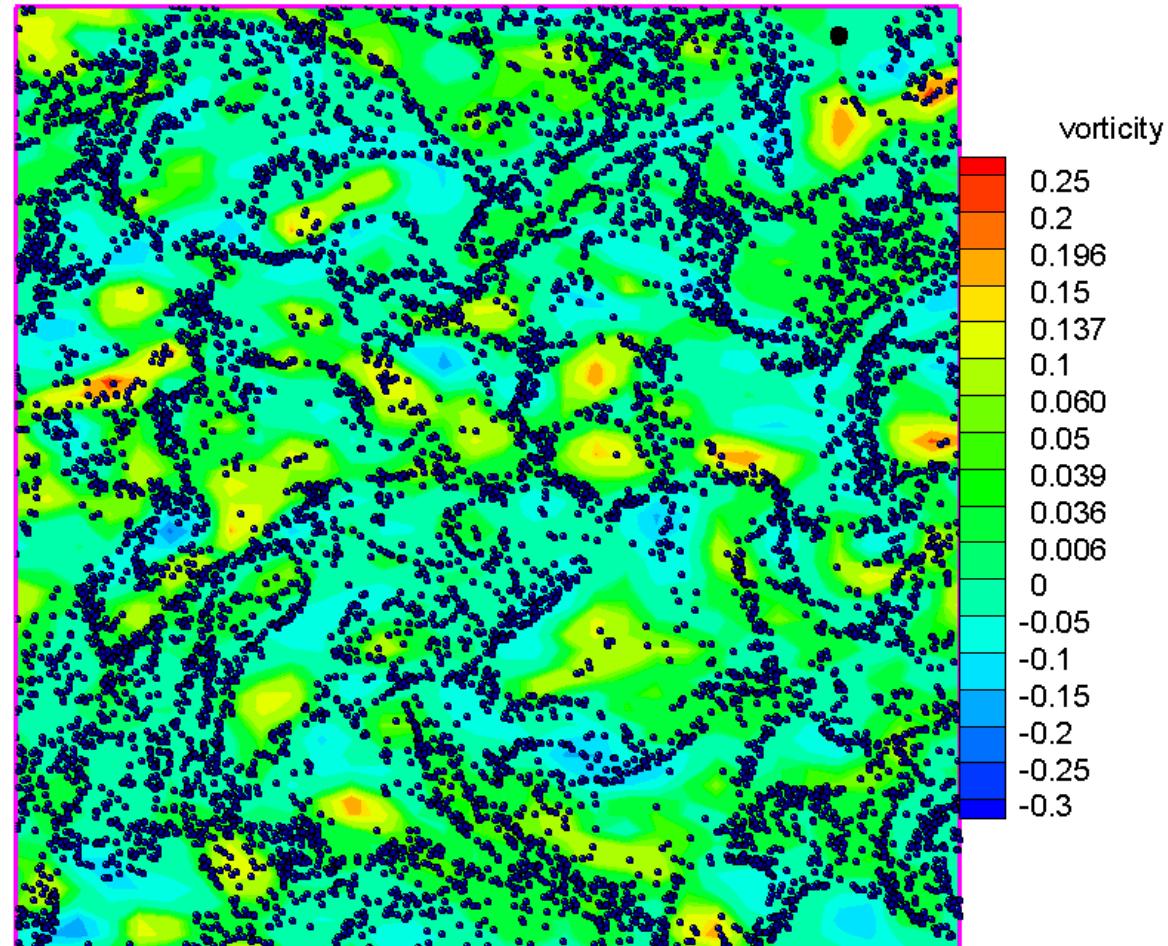


# Particle Distribution and Vorticity Contours

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Channel  
Center Plane

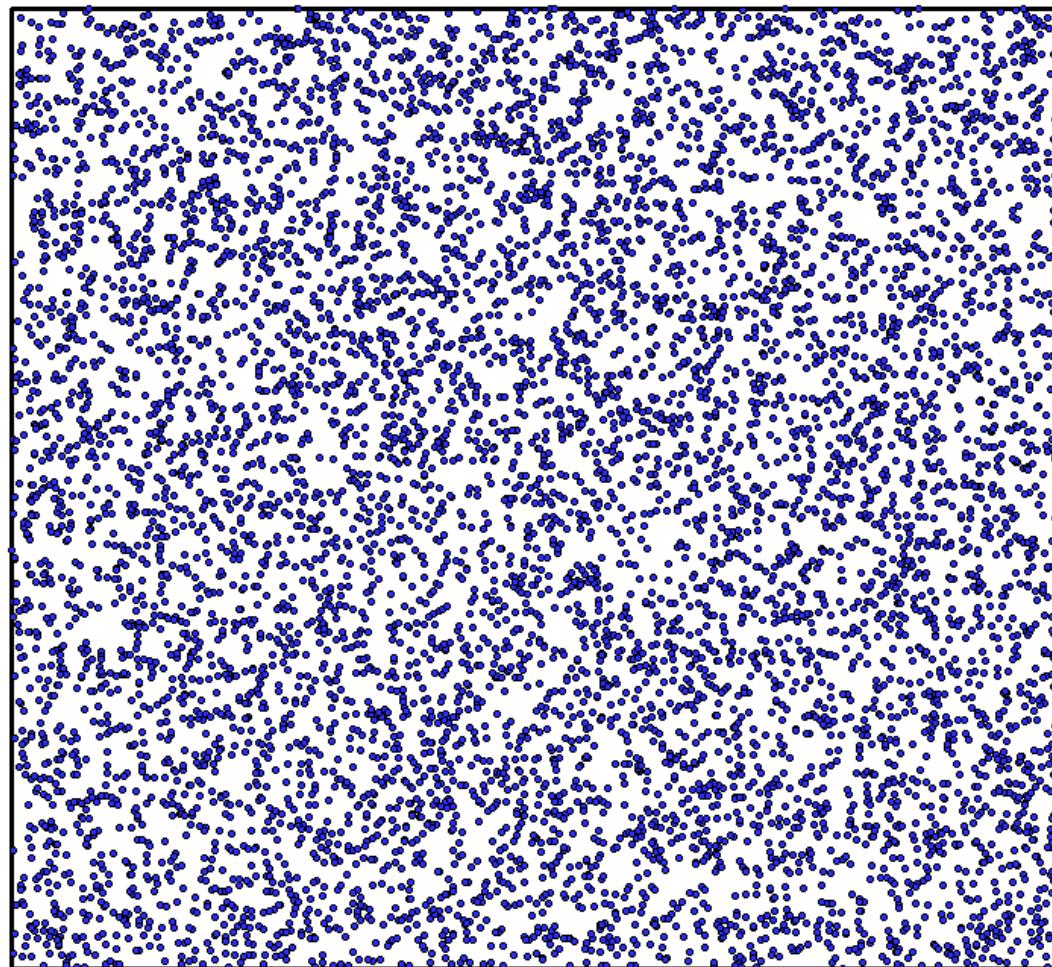
$$\tau_p^+ = 10.0$$



# Particle Distribution at the channel center-plane

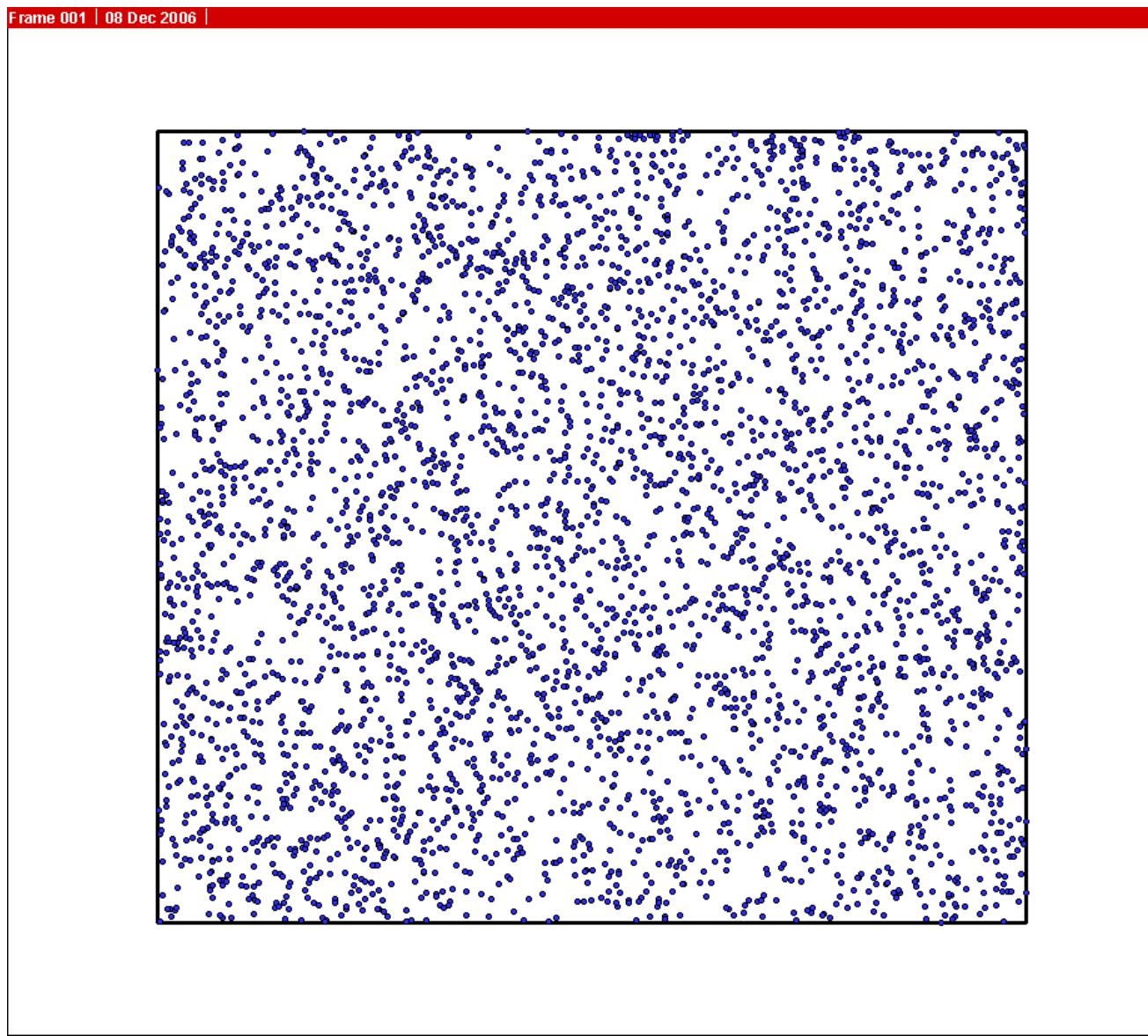
$\tau_p^+ = 10.0$

Frame 001 | 06 Dec 2006 |

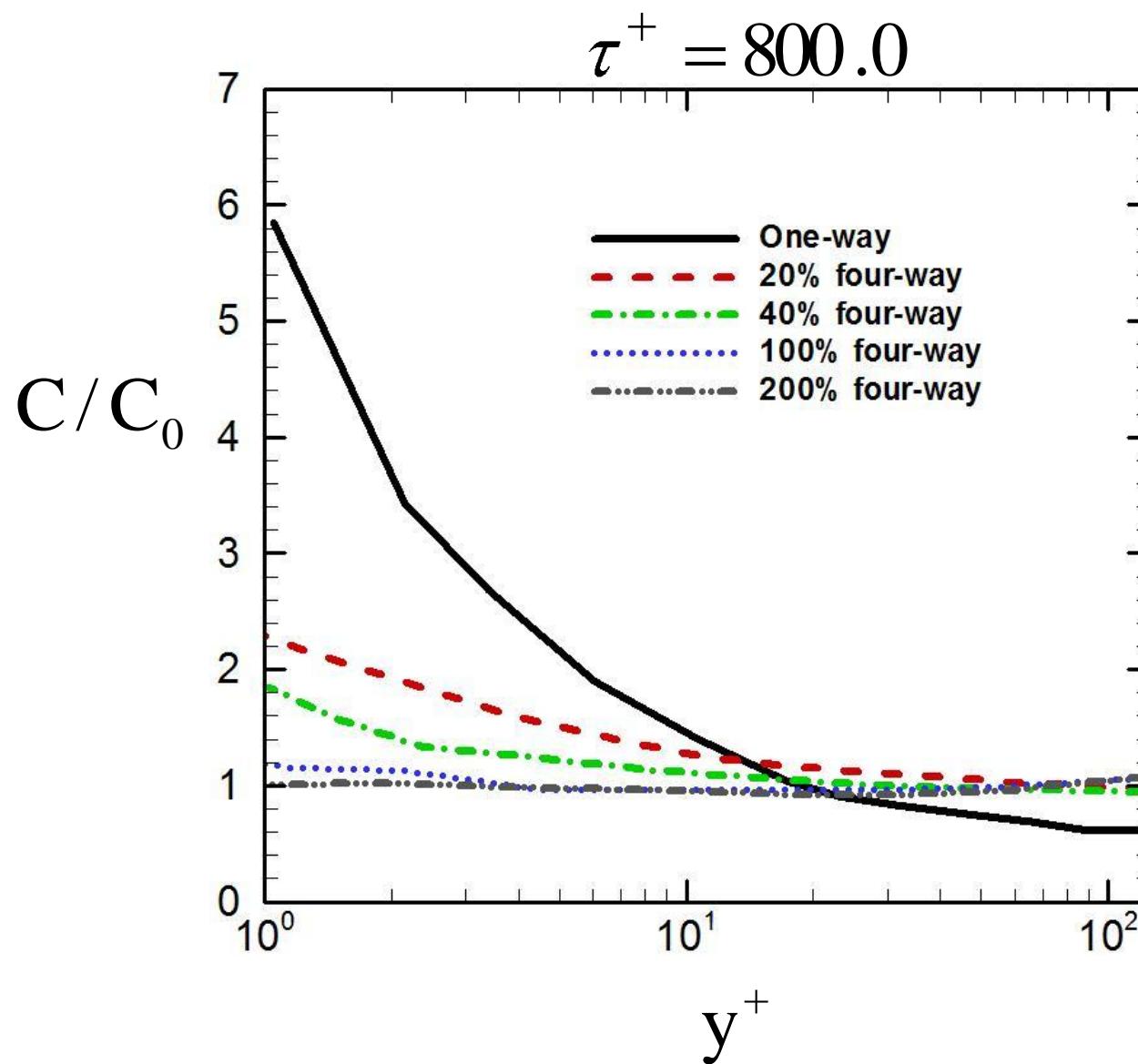


# Particle Distribution in the Wall Region

$$\tau_p^+ = 10.0$$



# Particle Concentration Profiles

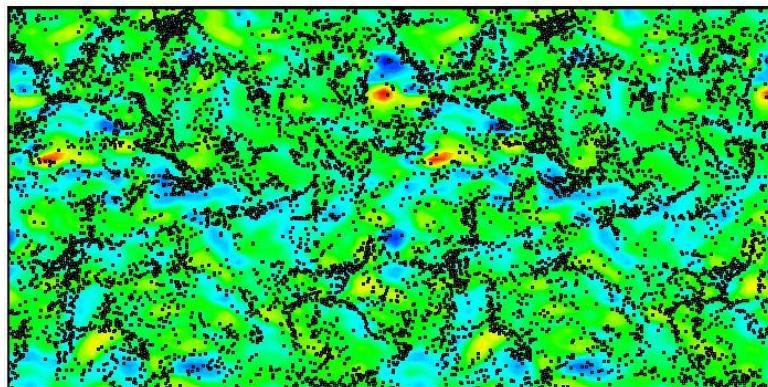
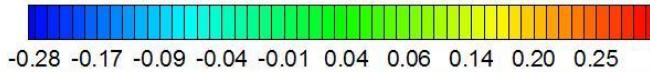


# Particle Distribution at the channel center-plane

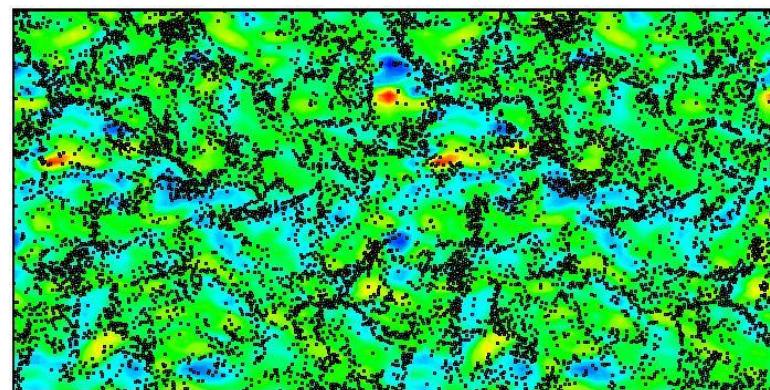
One-way

$$\tau^+ = 20.0$$

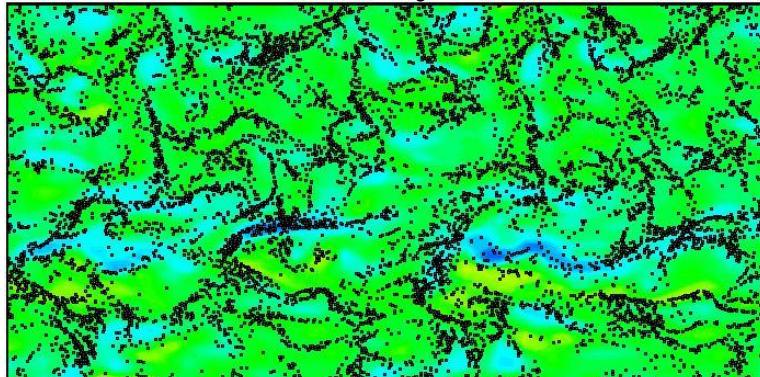
M.L. = 40%



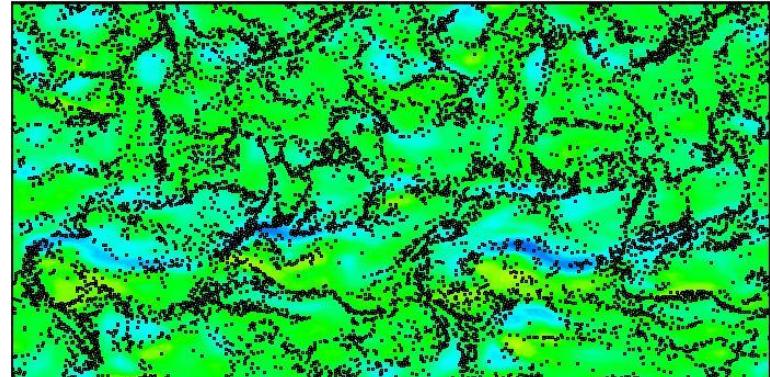
Collisions only



Two-way



Four-way



# Particle Distribution in the Wall Region

$$\tau^+ = 20.0$$

One-way

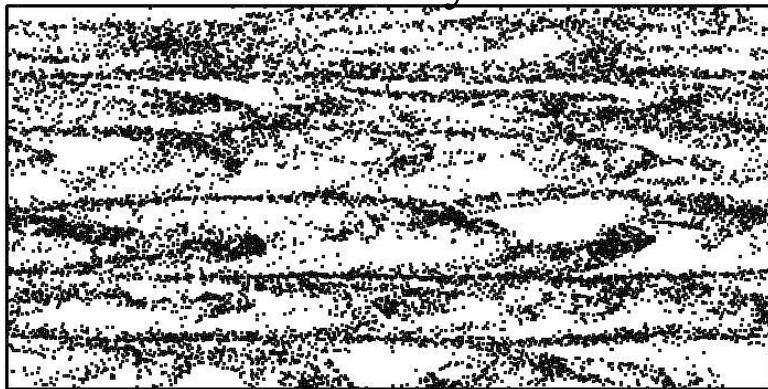


$$\text{M.L.} = 40\%$$

Collisions Only



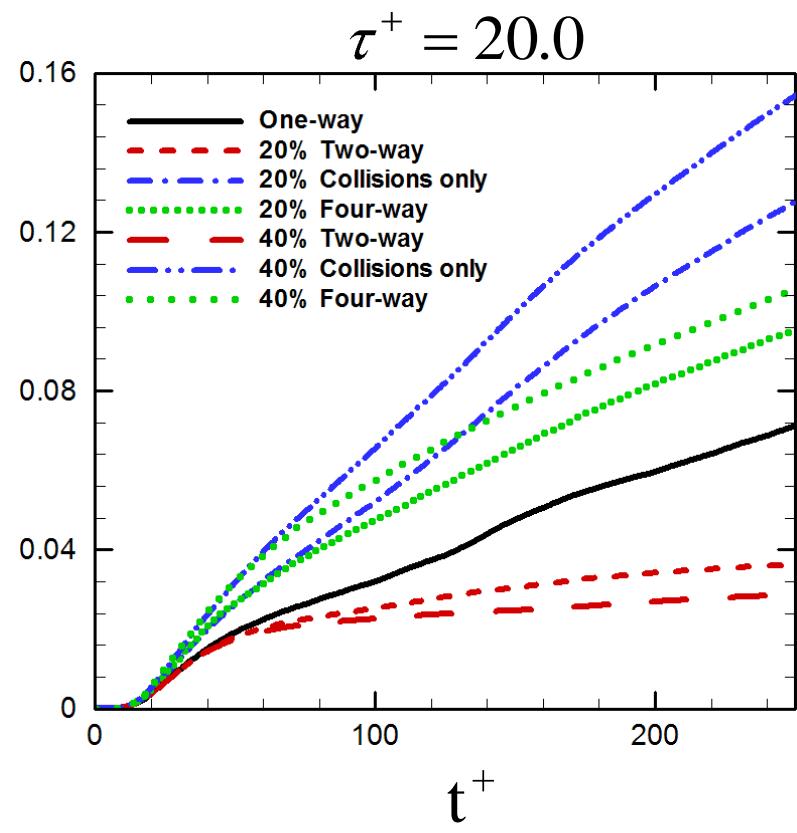
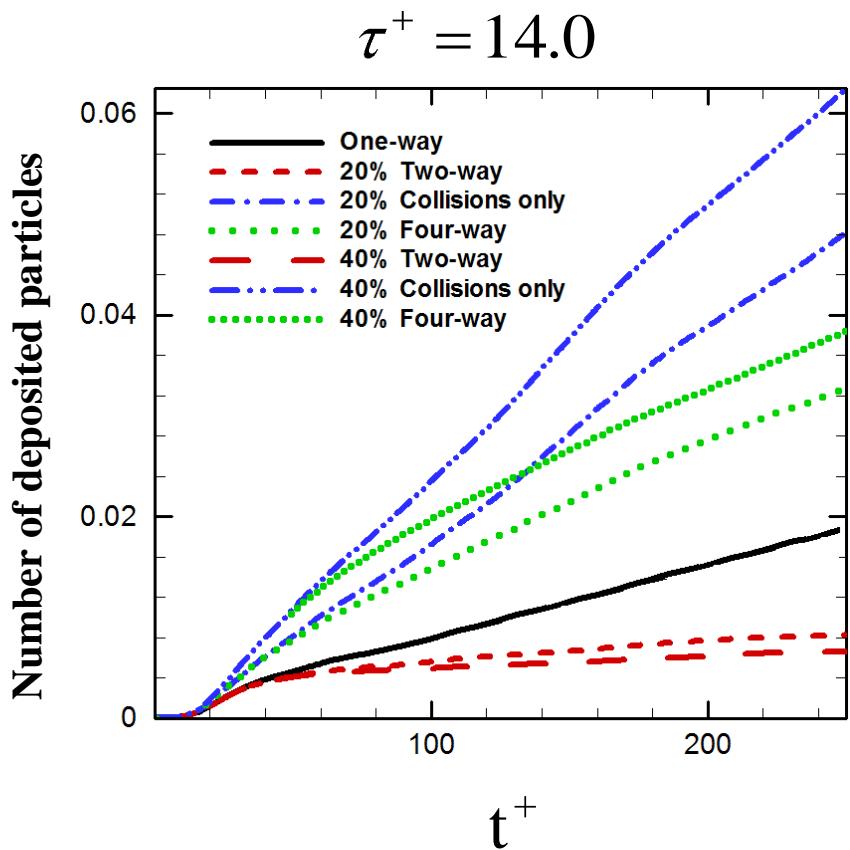
Two-way



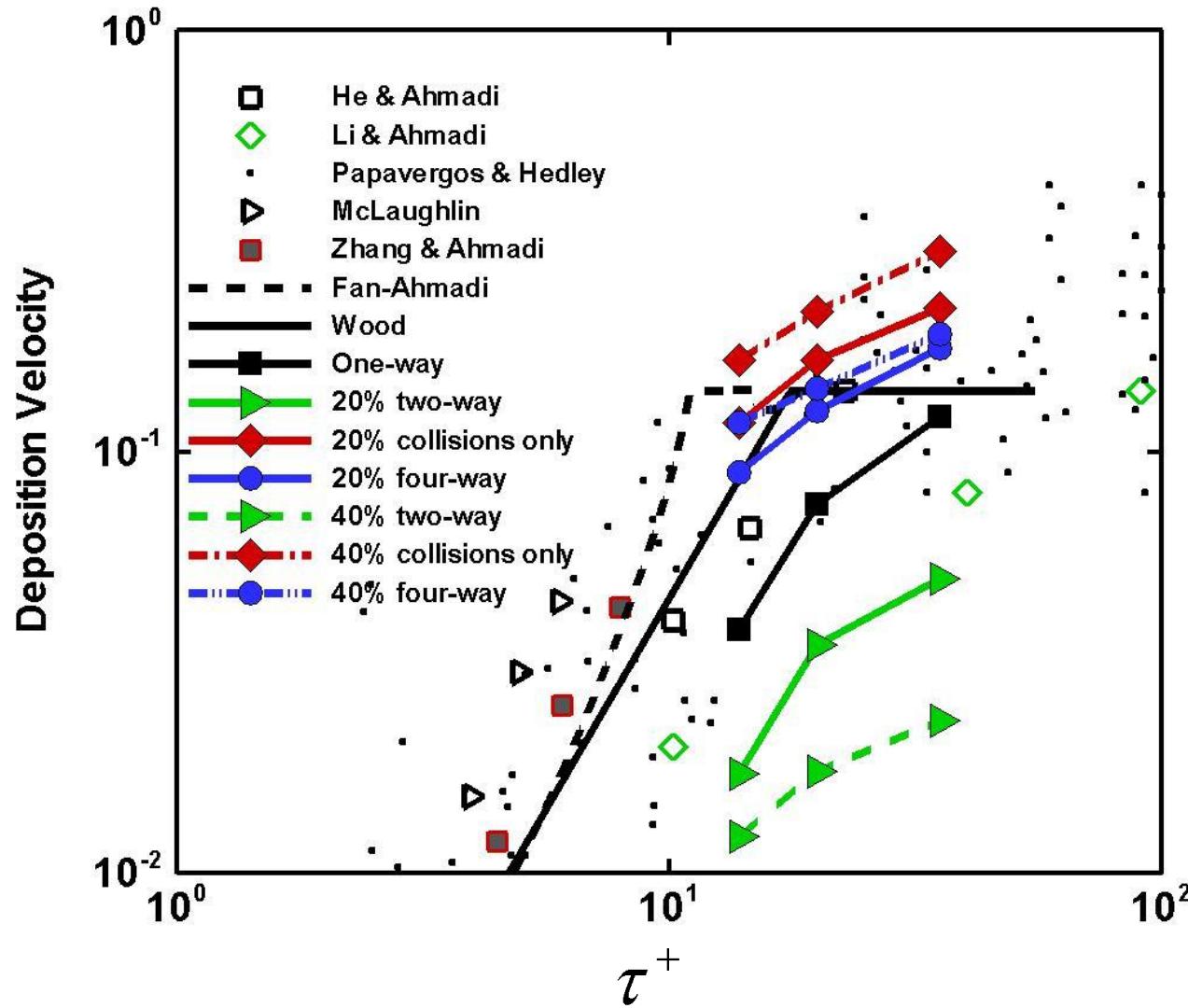
Four-way



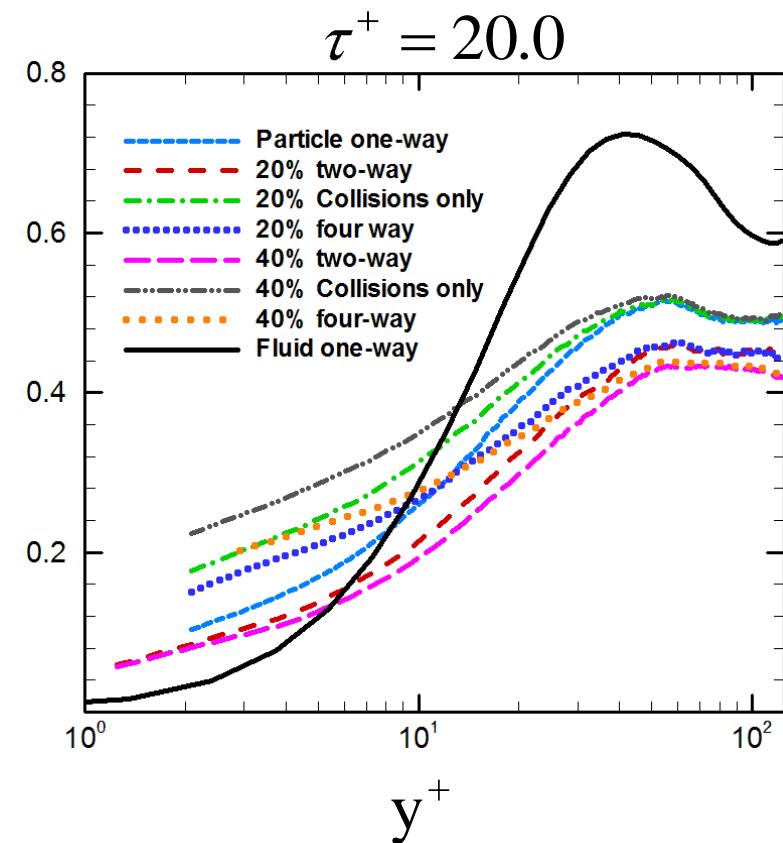
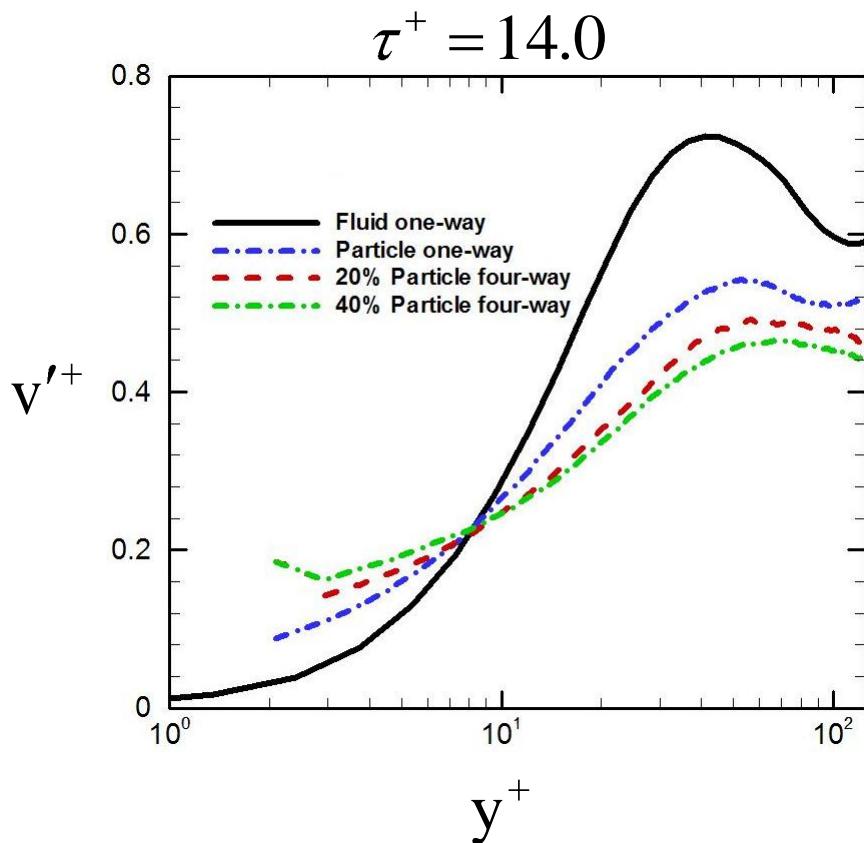
# Numerber of Deposited Particles Versus Time



# Particle Deposition Velocity

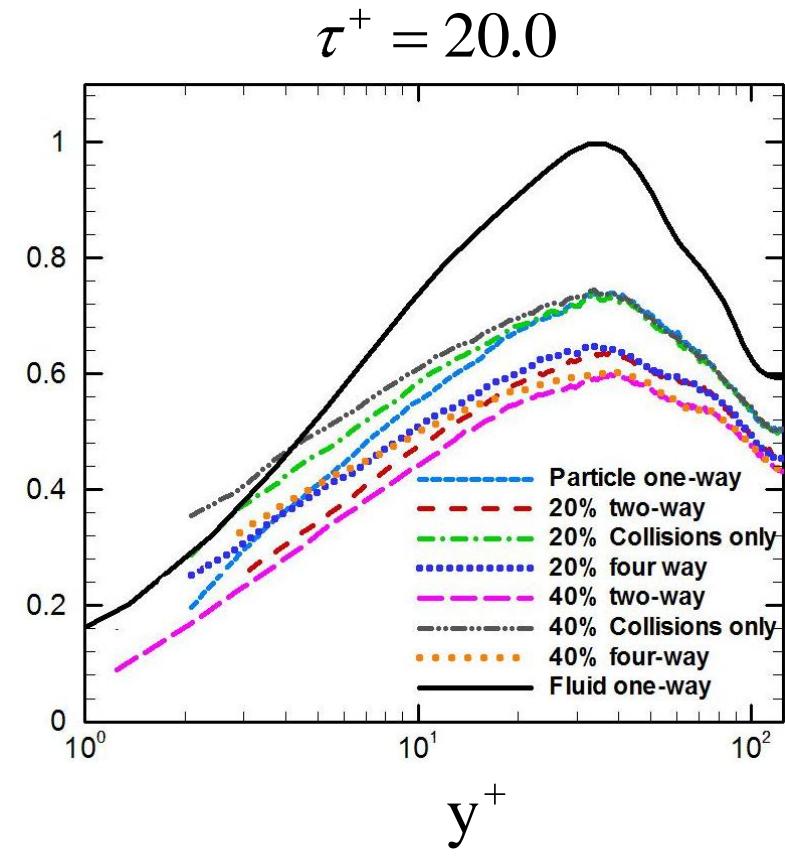
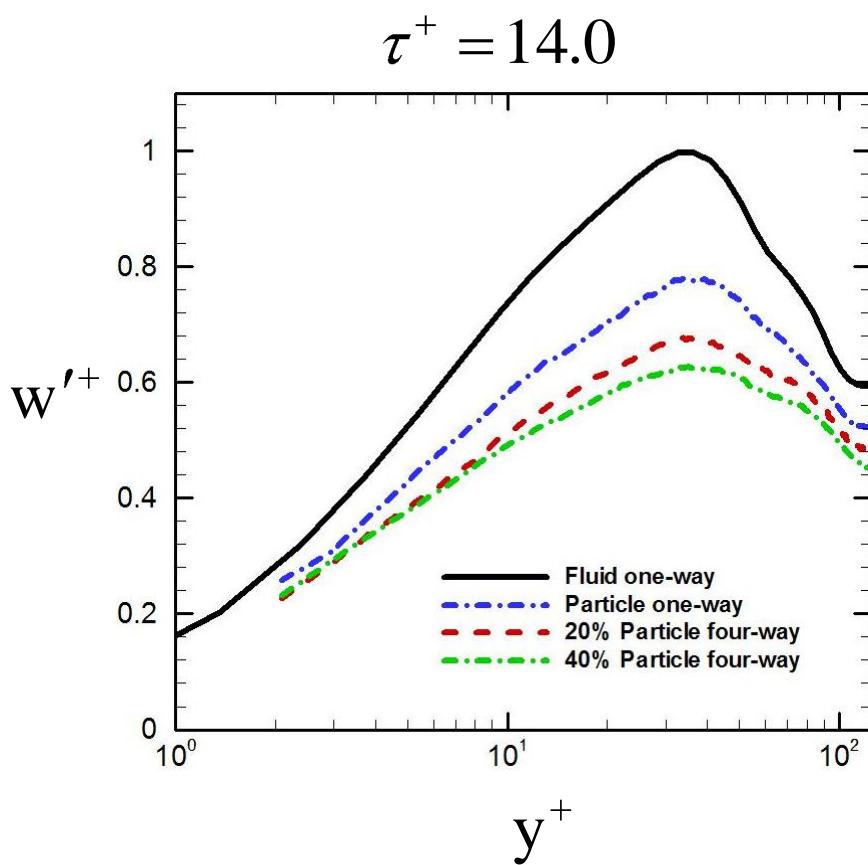


# Particle Normal Fluctuating Velocity



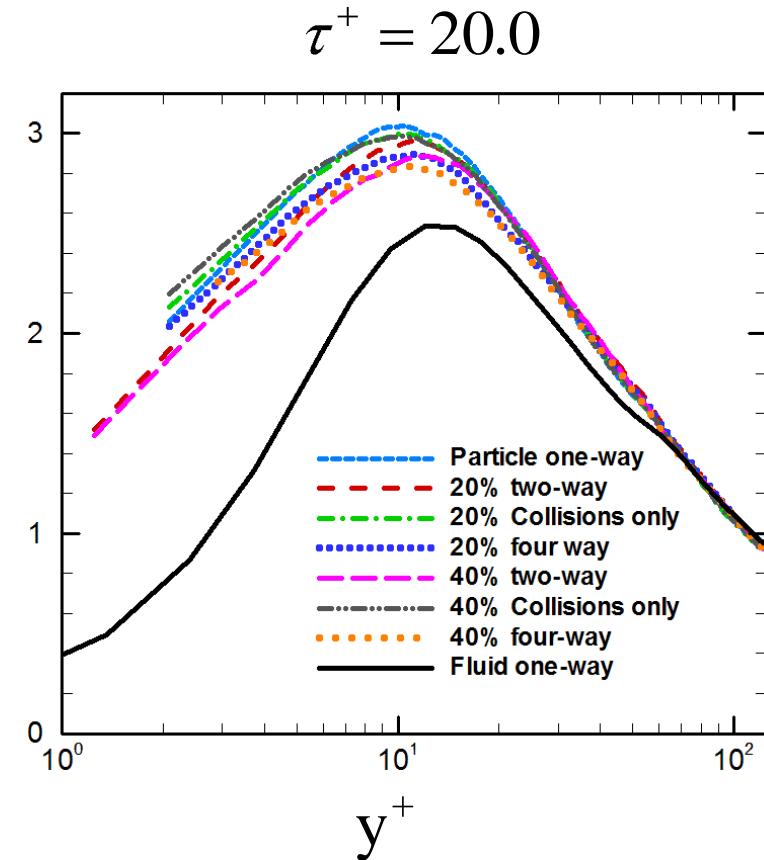
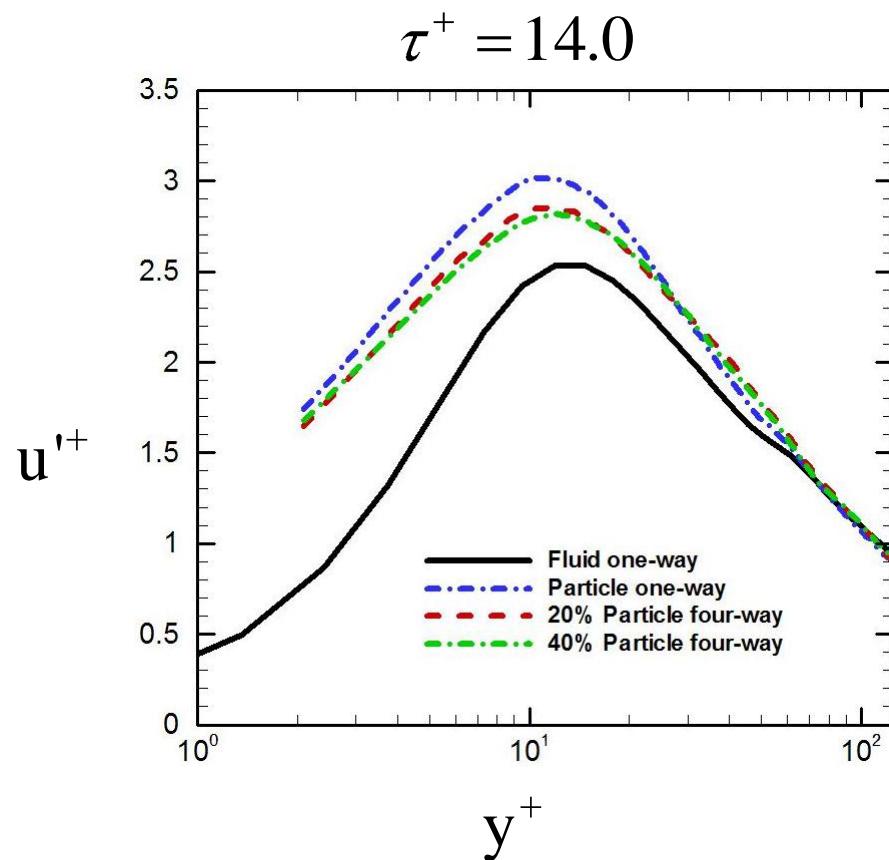
# Particle Spanwise Fluctuating Velocity

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# Particle Streamwise Fluctuating Velocity

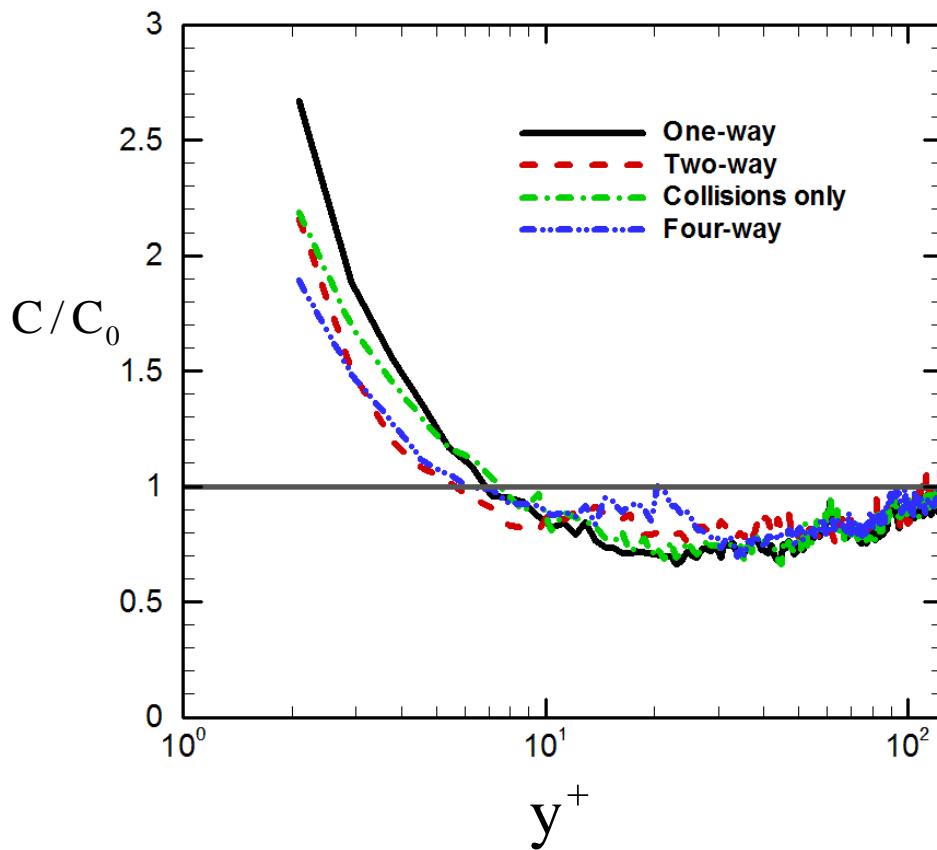
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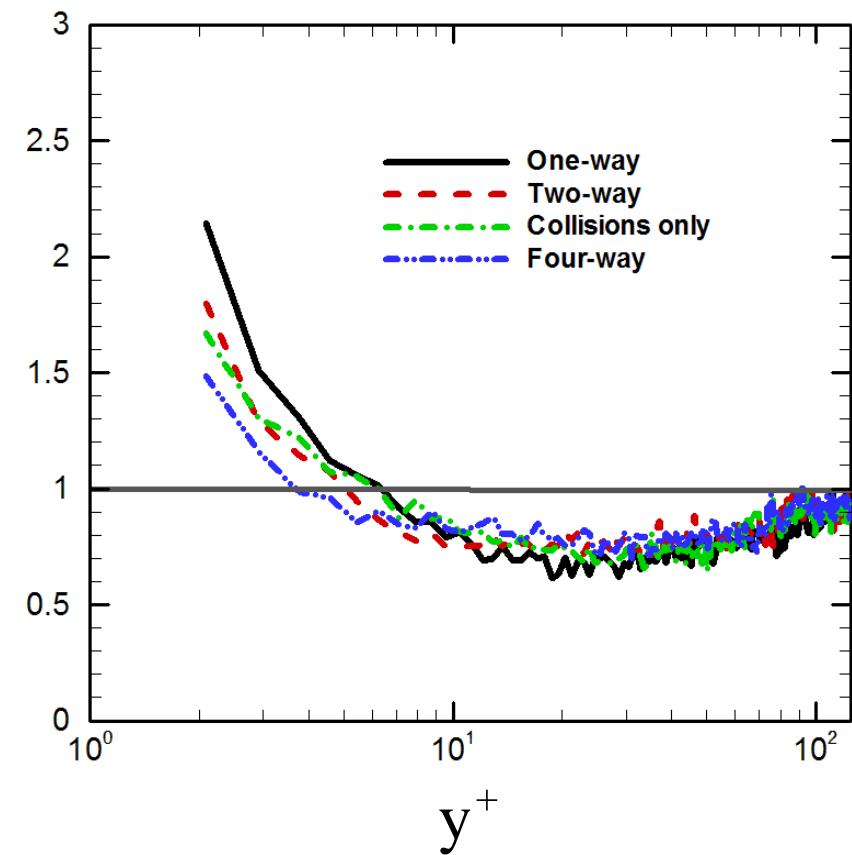
# Particle Concentration Profiles

**Mass Loading = 20%**

$\tau^+ = 14.0$



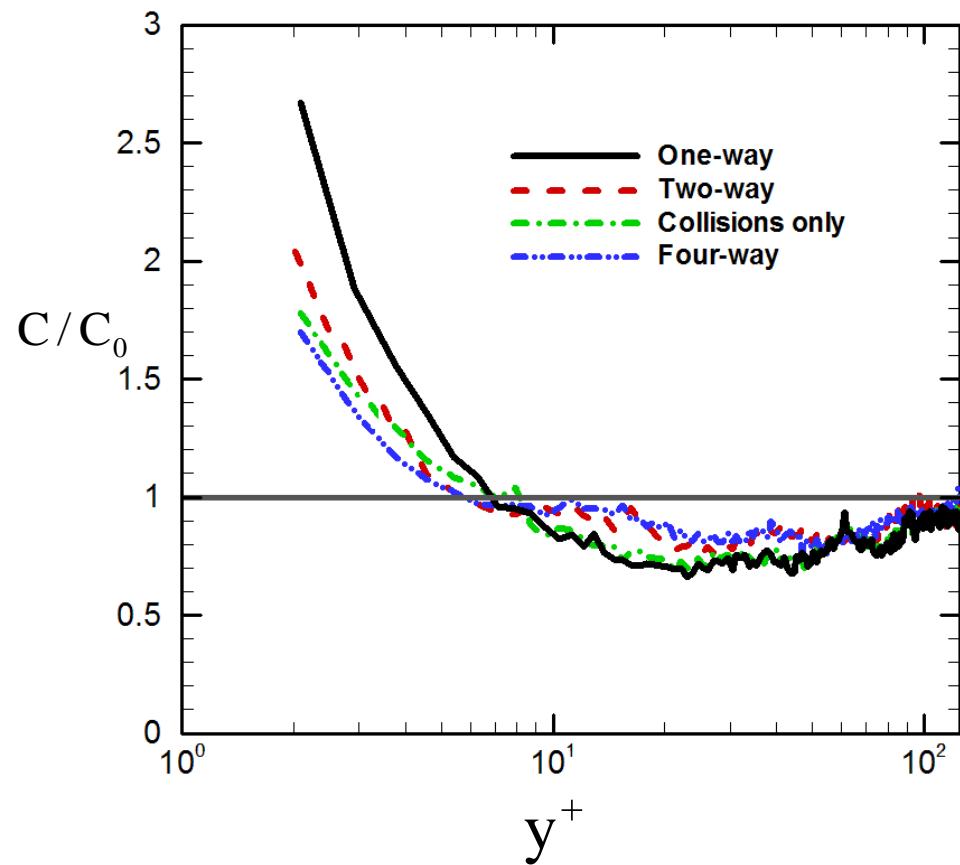
$\tau^+ = 20.0$



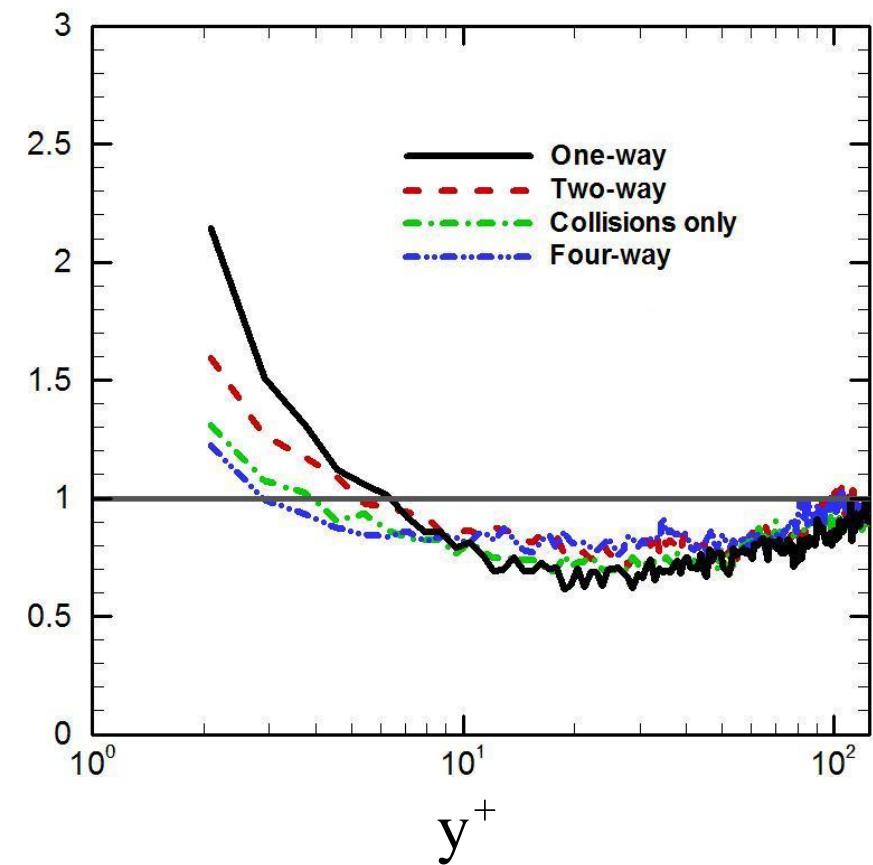
# Particle Concentration Profiles

Mass Loading = 40%

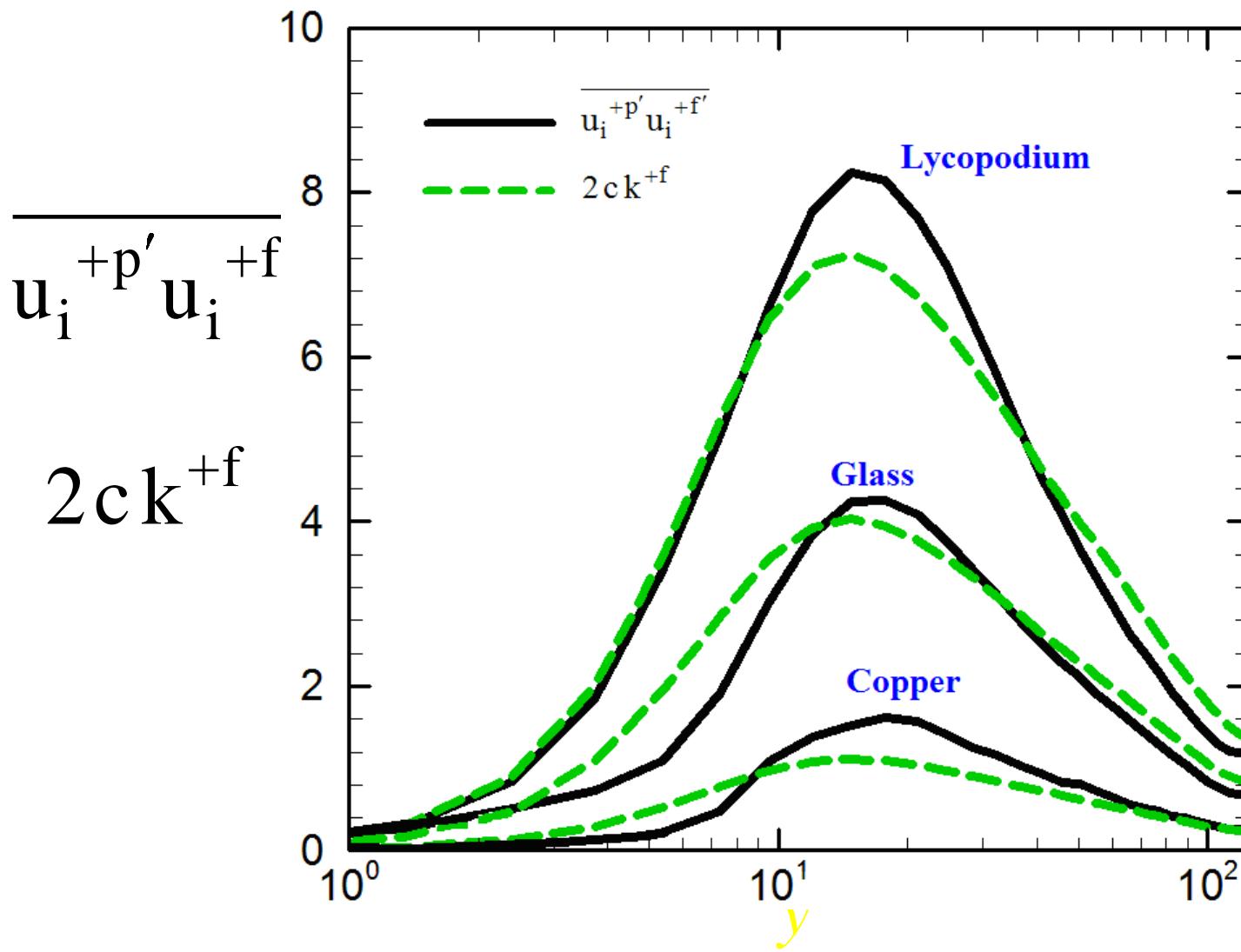
$\tau^+ = 14.0$



$\tau^+ = 20.0$



# Comparisons with Model



# Conclusions

- **Turbulence coherent vortical near-wall structure plays an important role on the particle deposition concentration profiles.**
- **Presence of particles attenuates the intensity of the fluid fluctuations, and as particle mass loading increases, the level of attenuation increases.**
- **Inter-particle collisions increases the particle deposition velocity while two-way coupling decreases it.**
- **Inter-particle collisions and two-way coupling reduce the particle accumulation near the wall.**

# Thank You!

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# Questions?

